

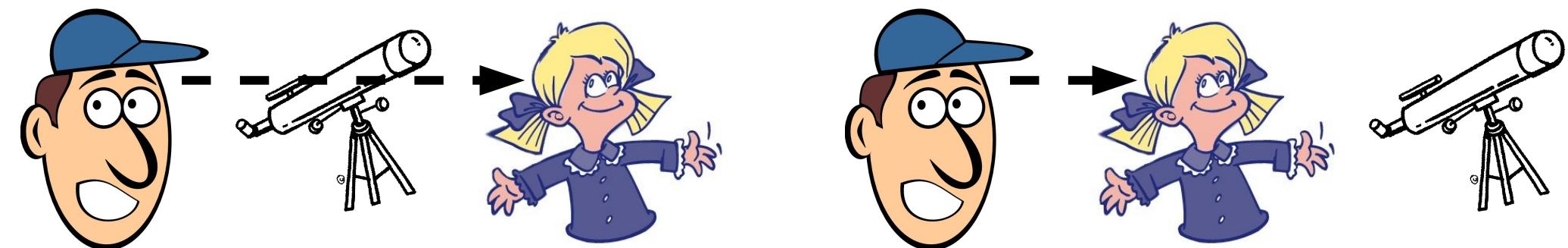
# NLP Programming Tutorial 8 - Phrase Structure Parsing

Graham Neubig

Nara Institute of Science and Technology (NAIST)

# Interpreting Language is Hard!

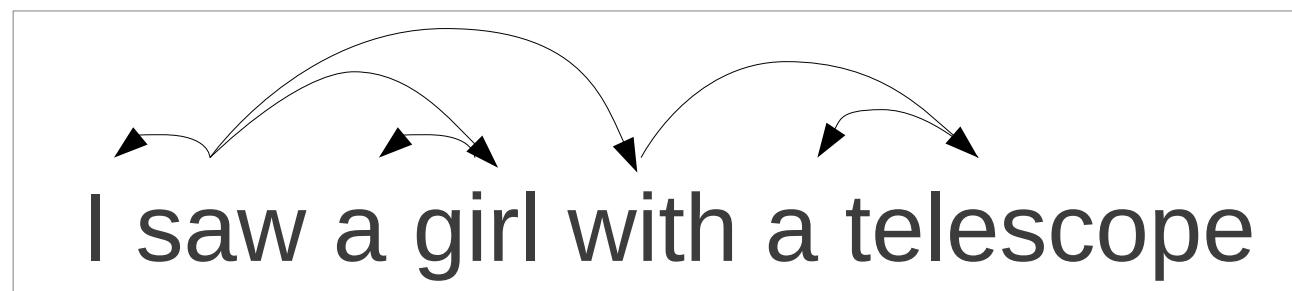
I saw a girl with a telescope



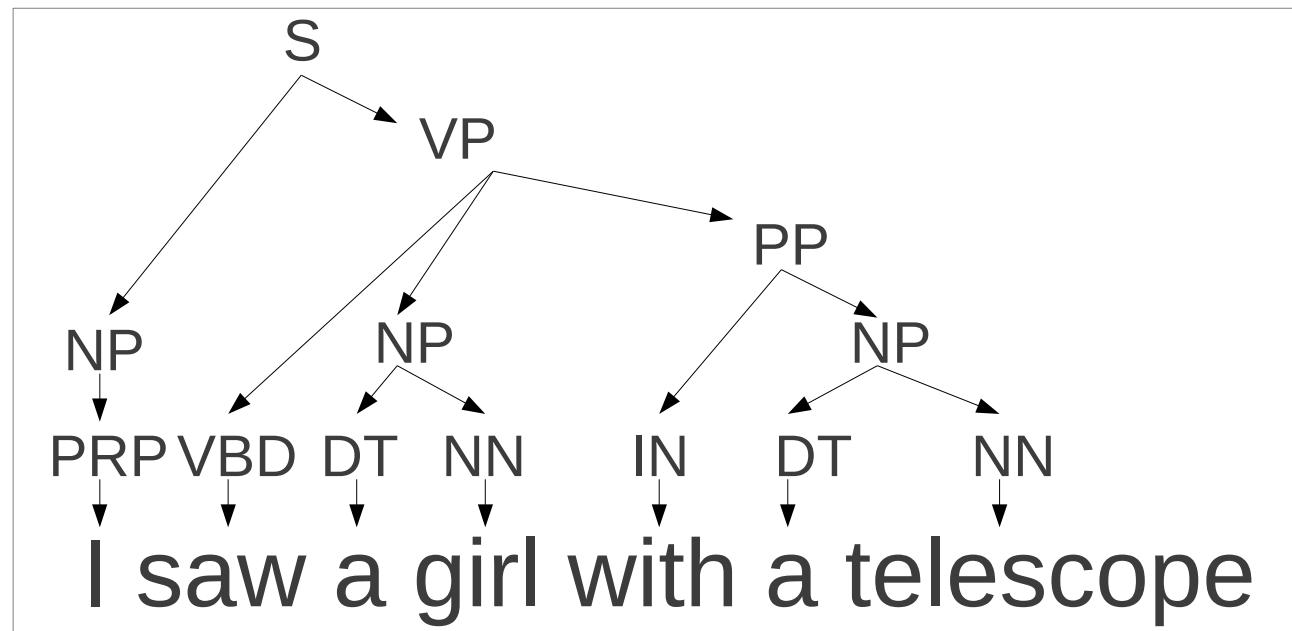
- “Parsing” resolves structural ambiguity in a formal way

# Two Types of Parsing

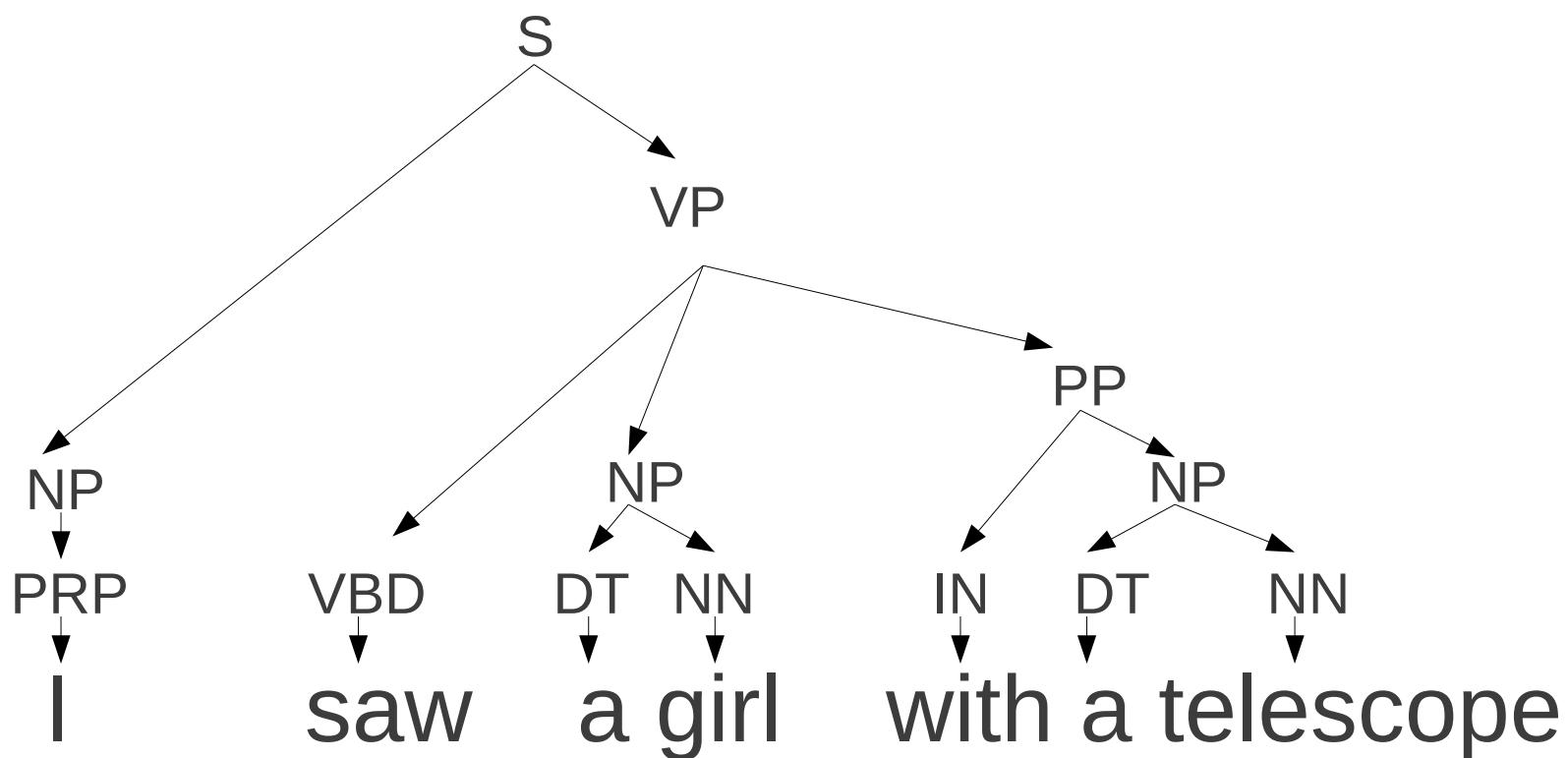
- **Dependency:** focuses on relations between words



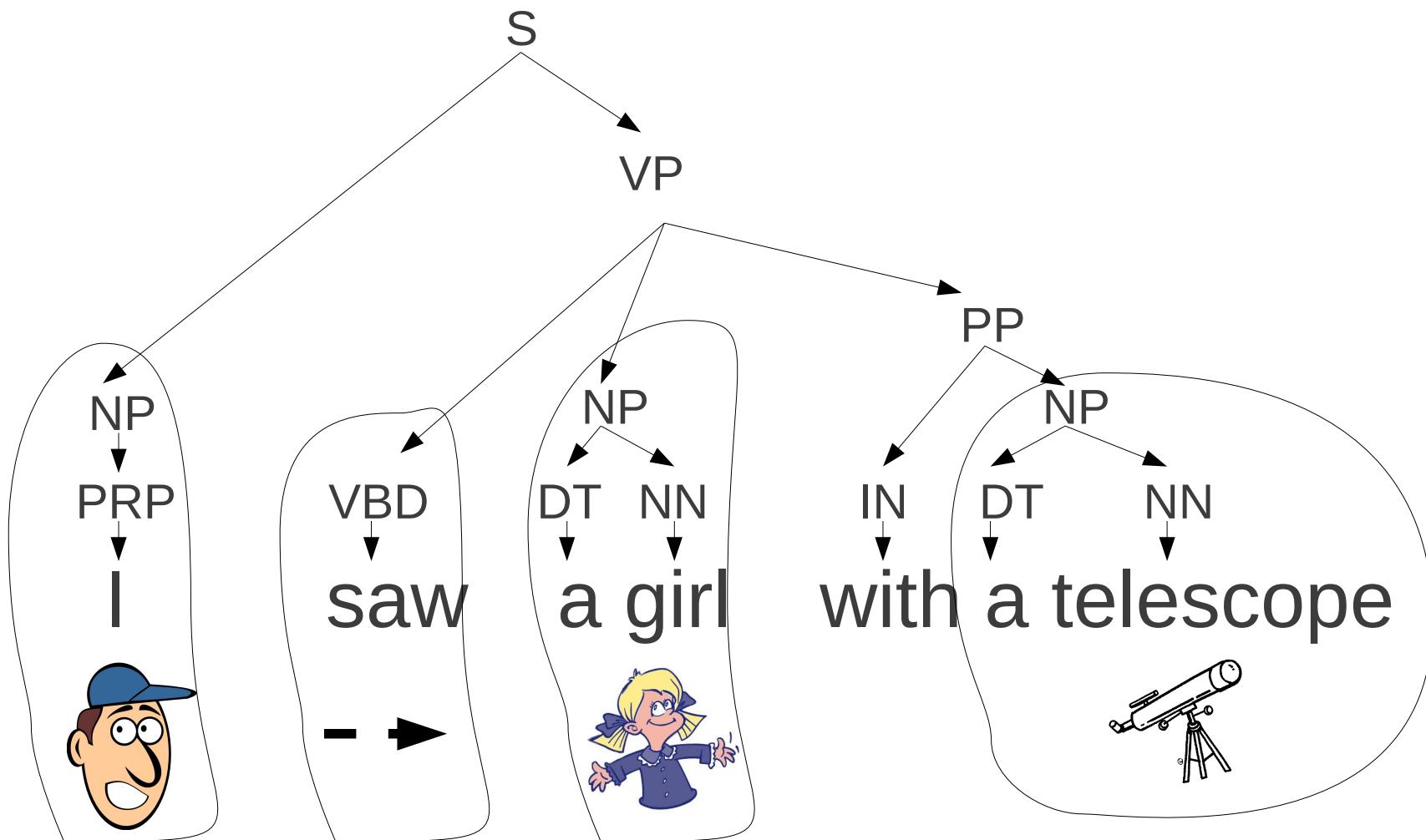
- **Phrase structure:** focuses on identifying phrases and their recursive structure



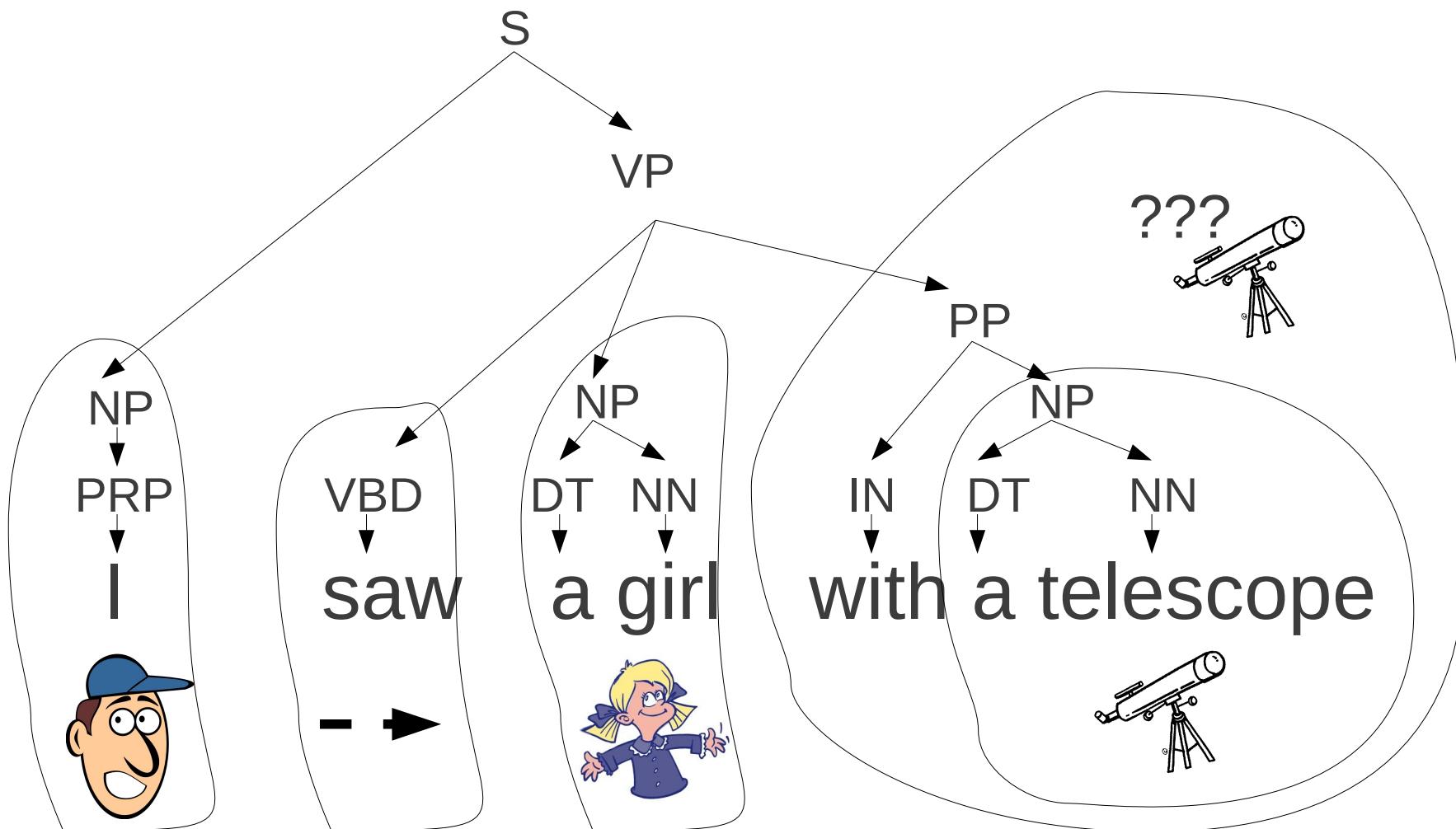
# Recursive Structure?



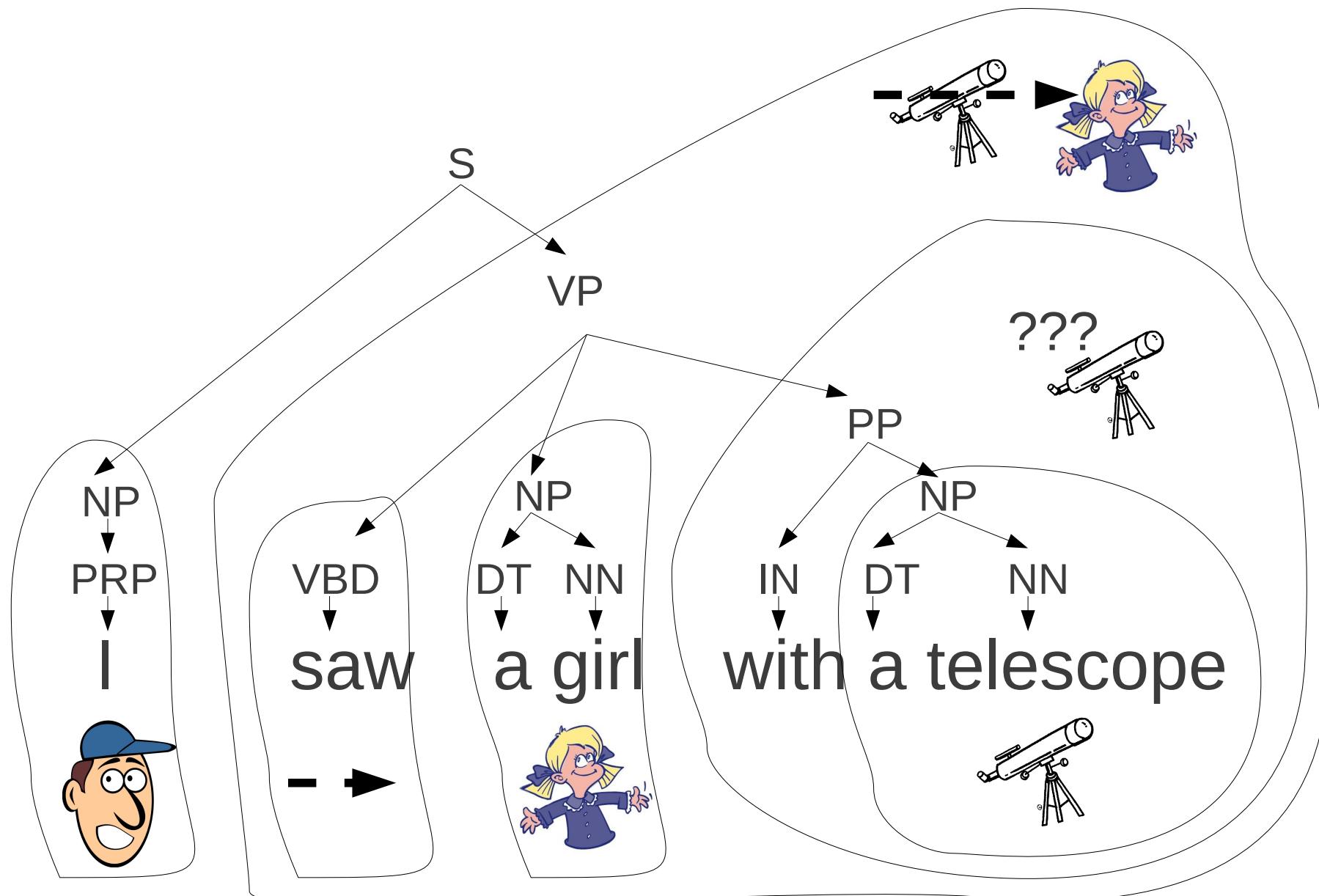
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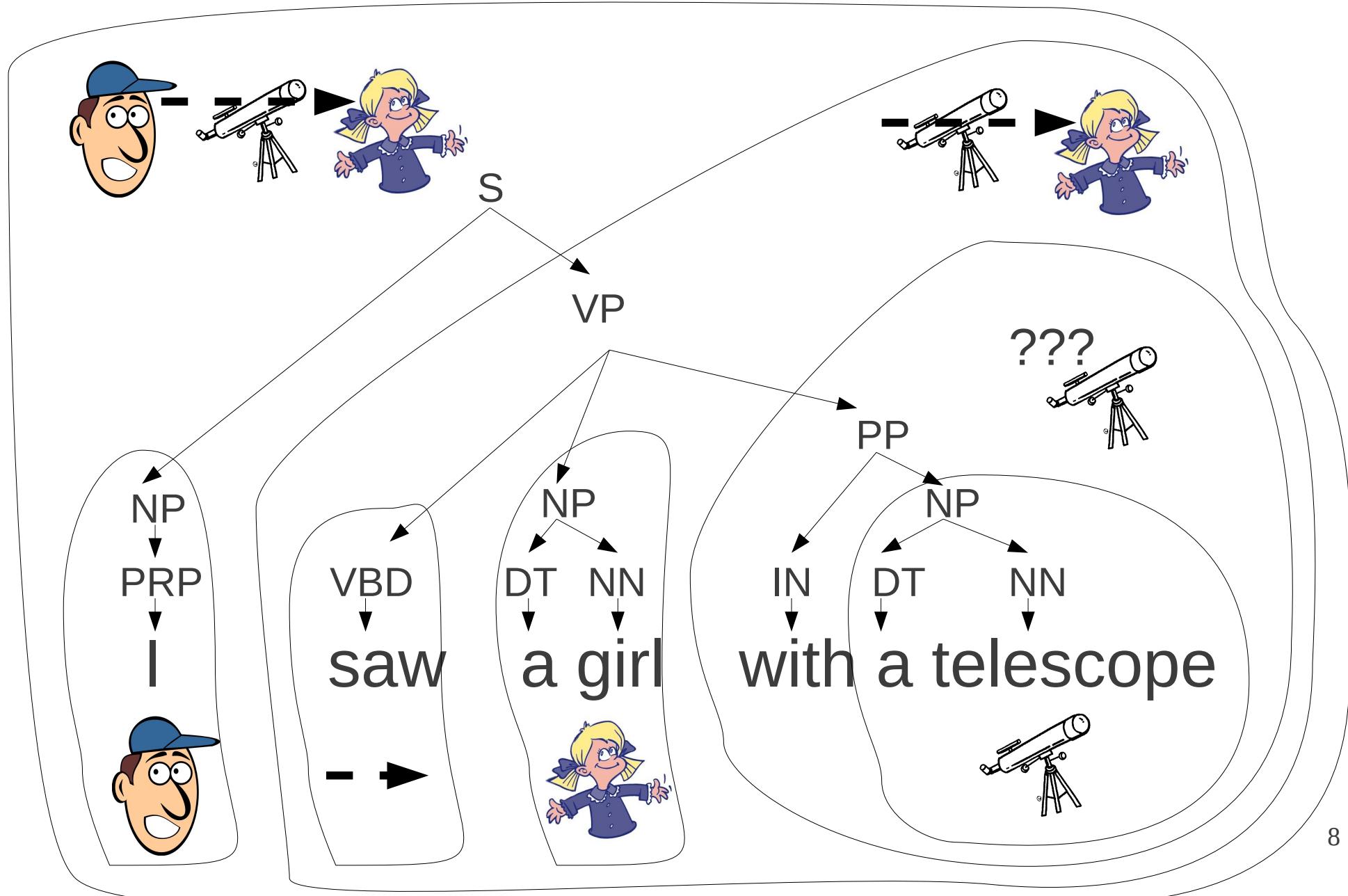
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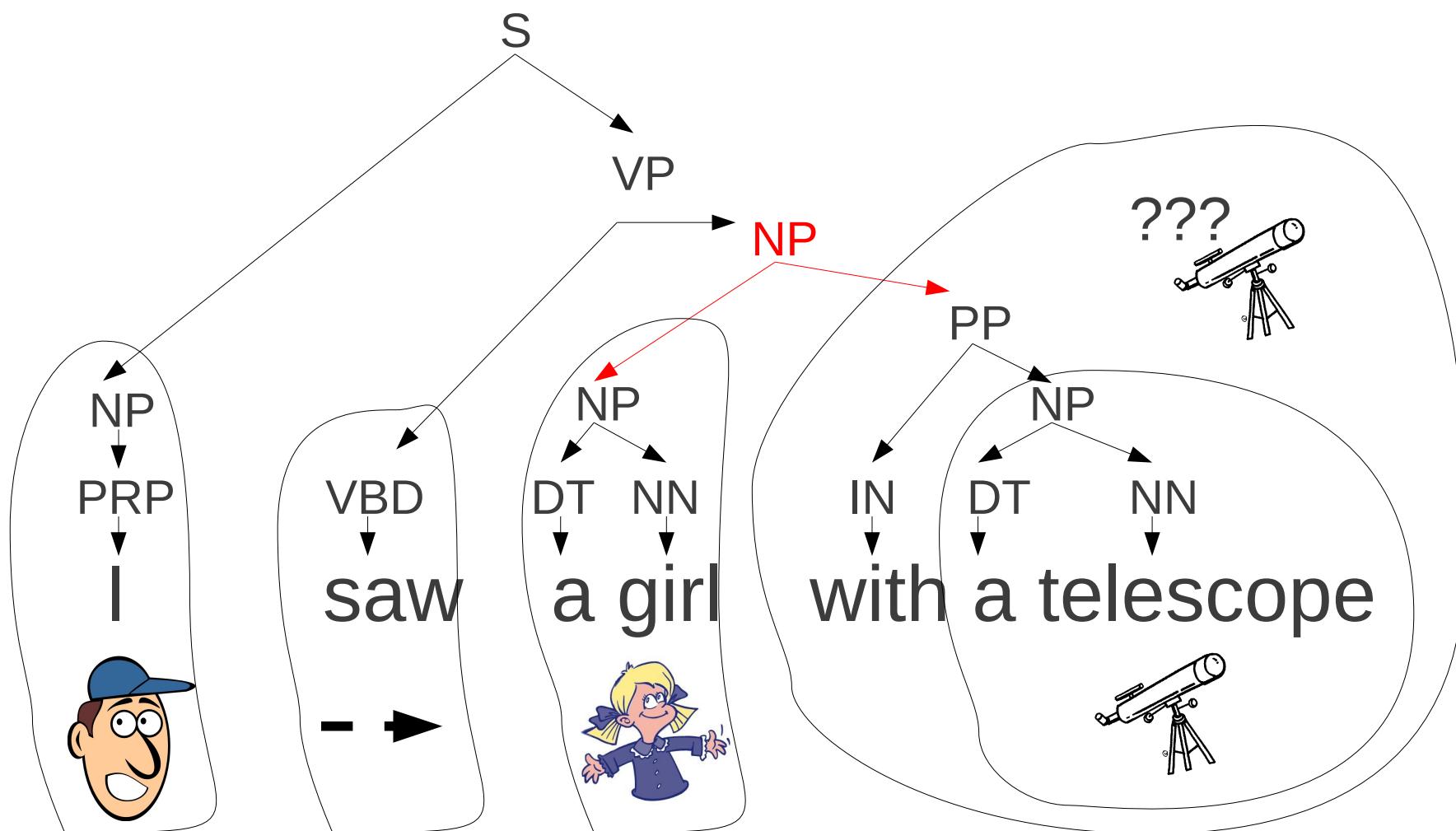
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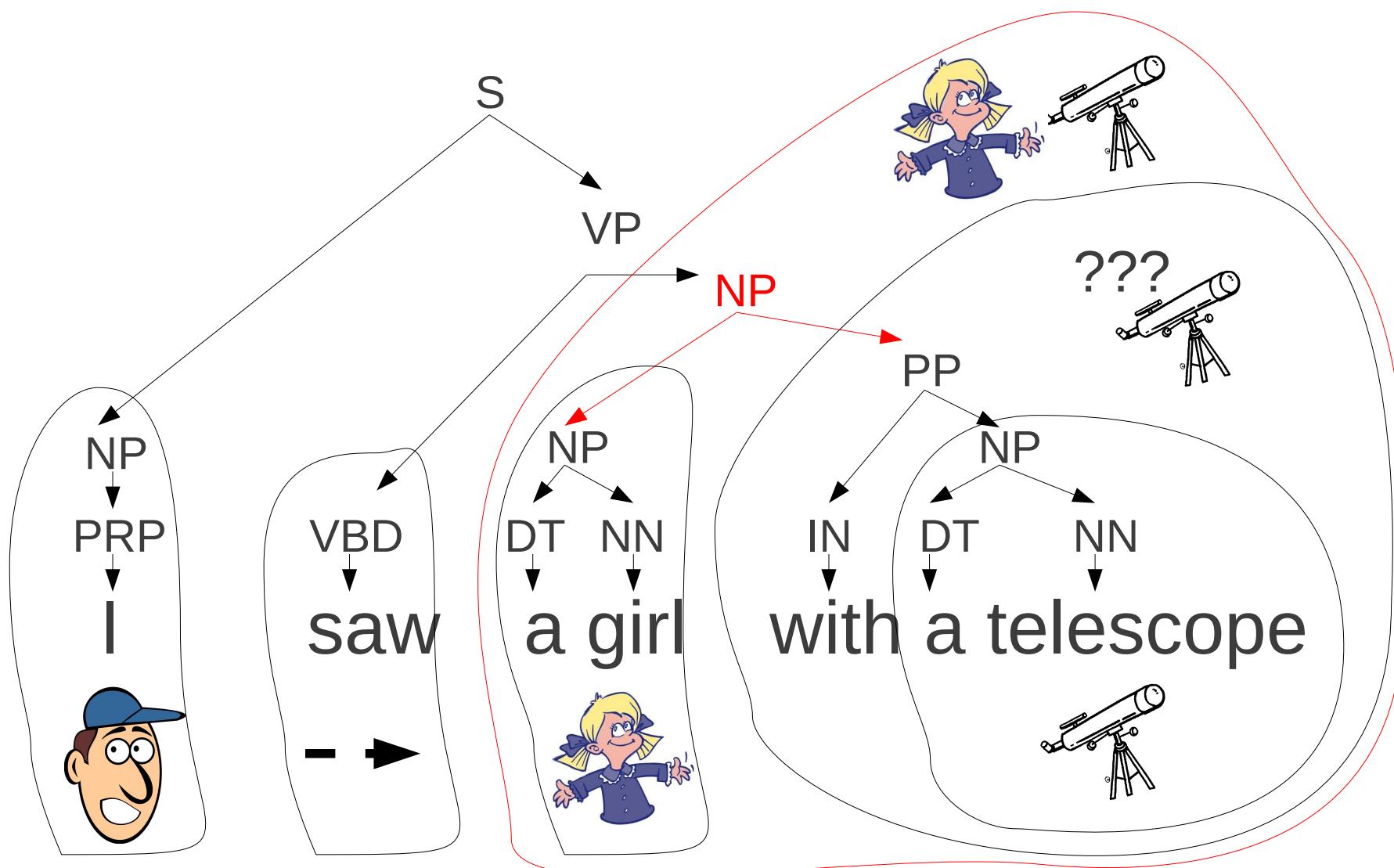
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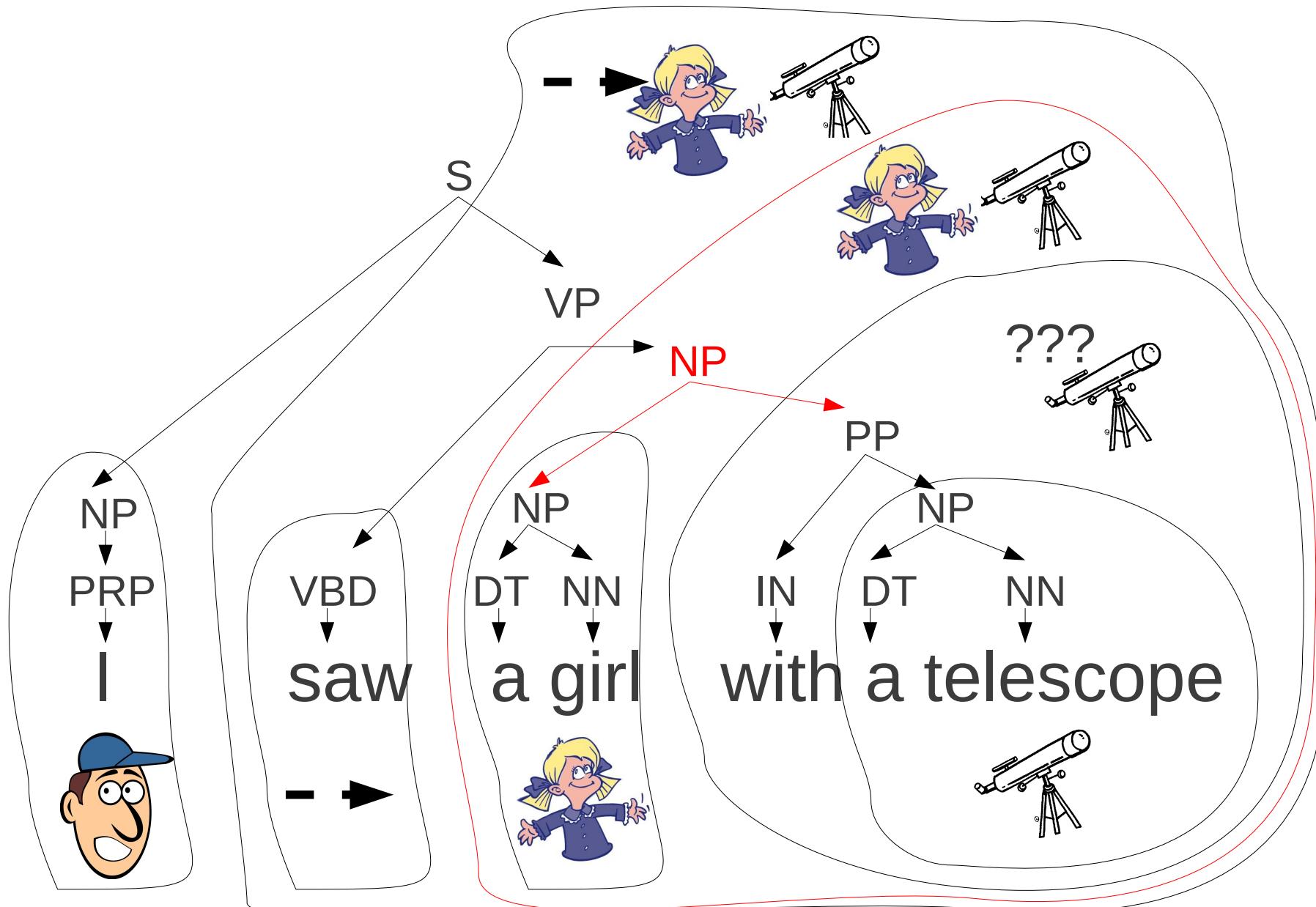
# Different Structure, Different Interpretation



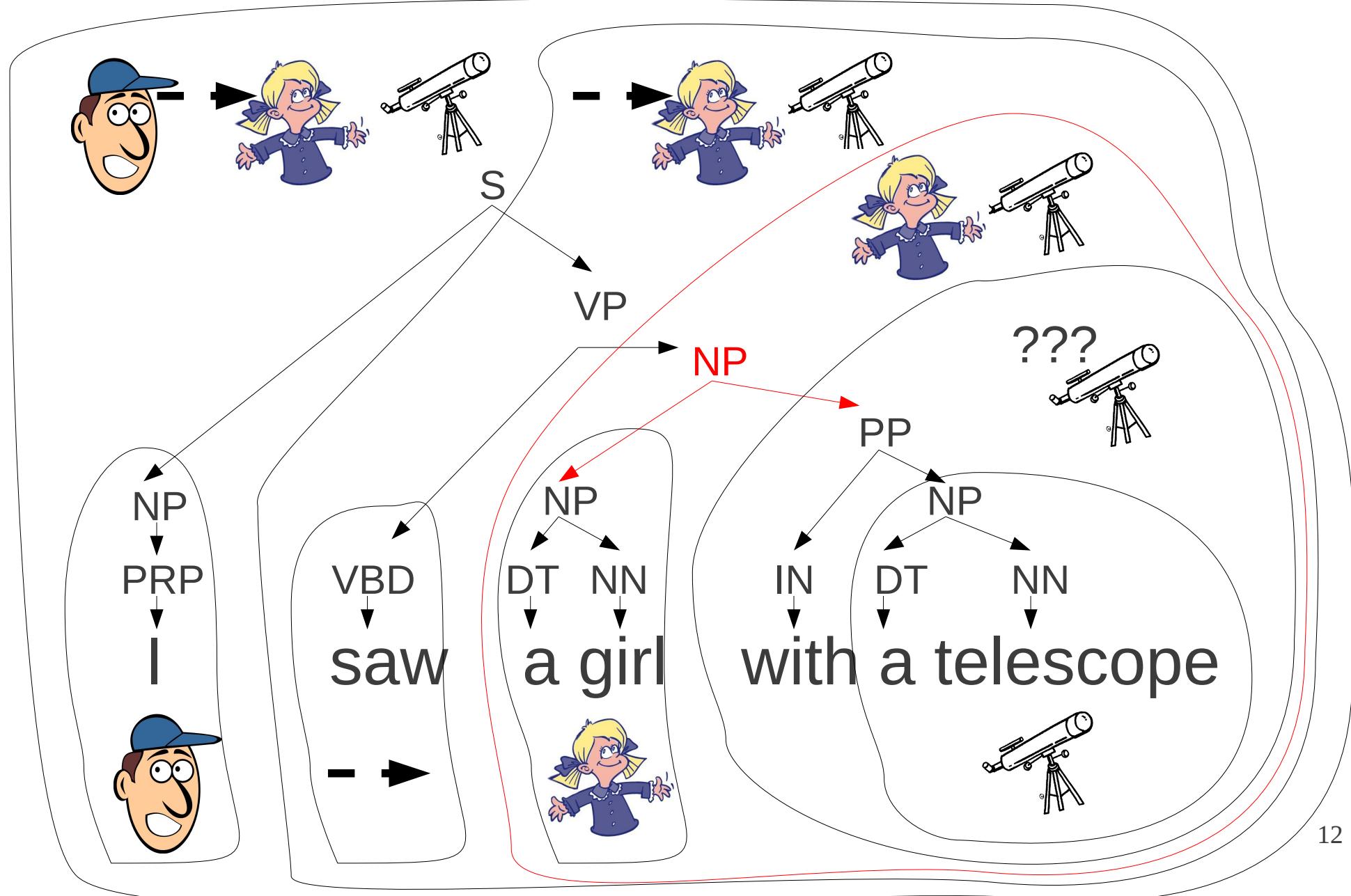
# Different Structure, Different Interpretation



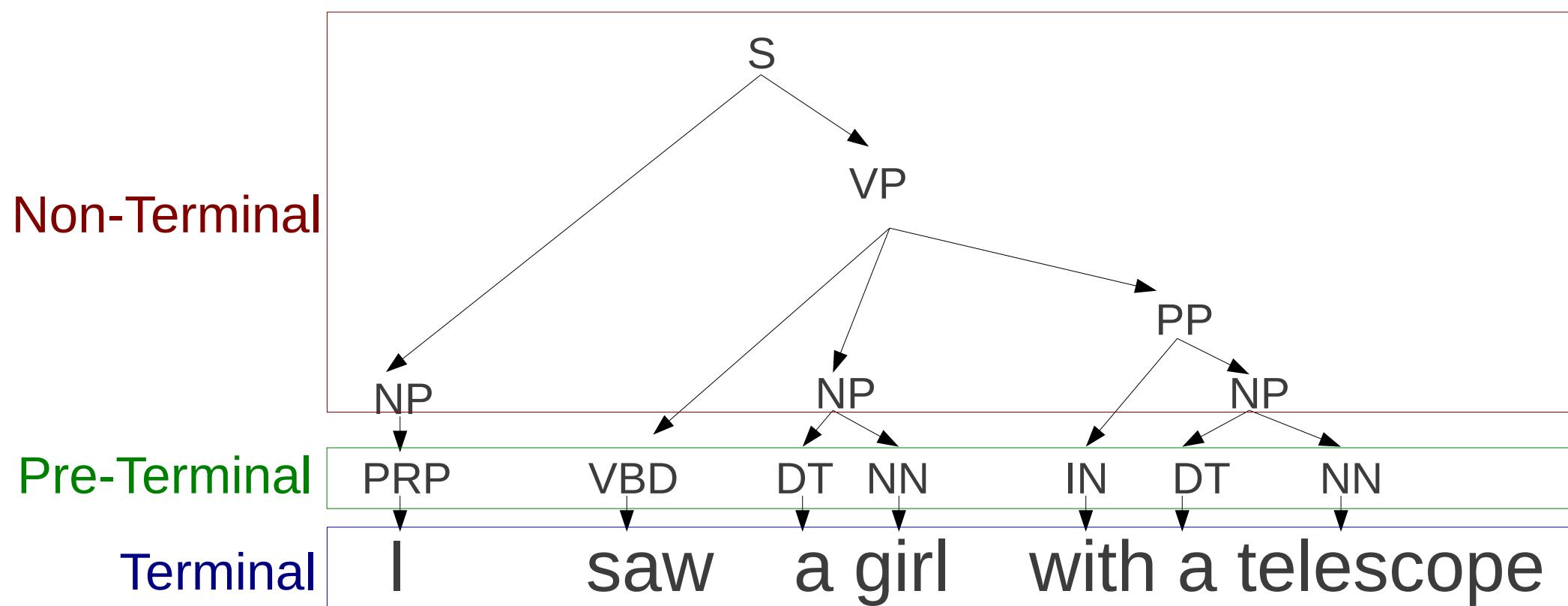
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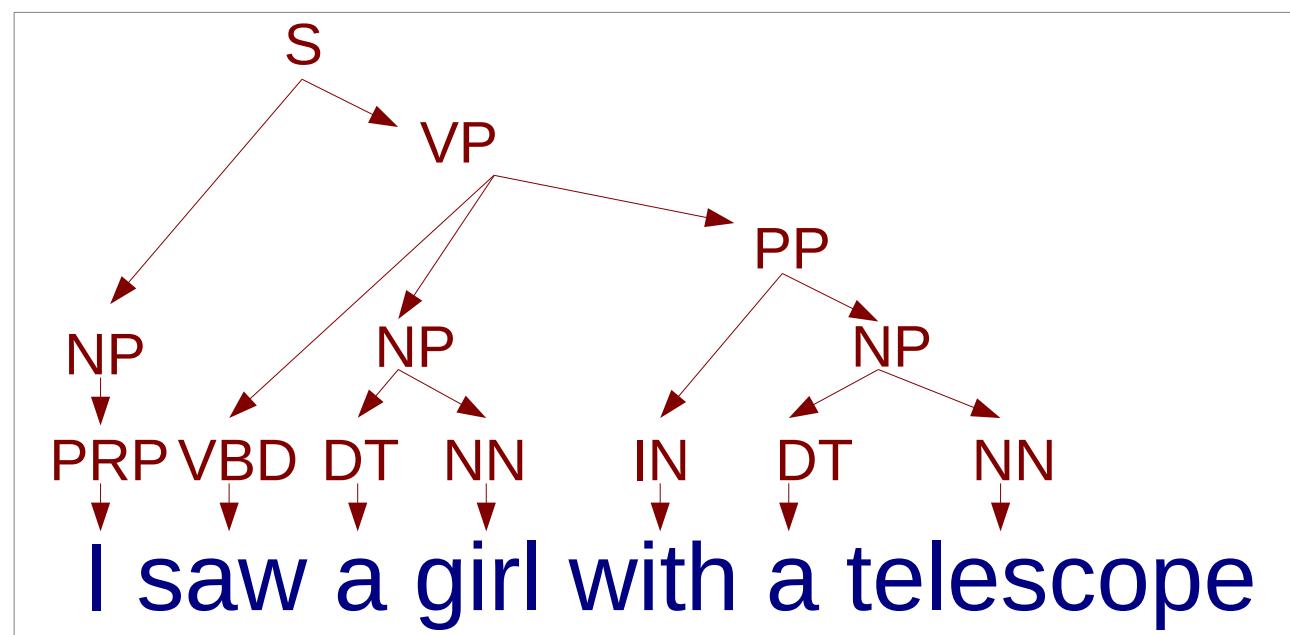


# Non-Terminals, Pre-Terminals, Terminals



# Parsing as a Prediction Problem

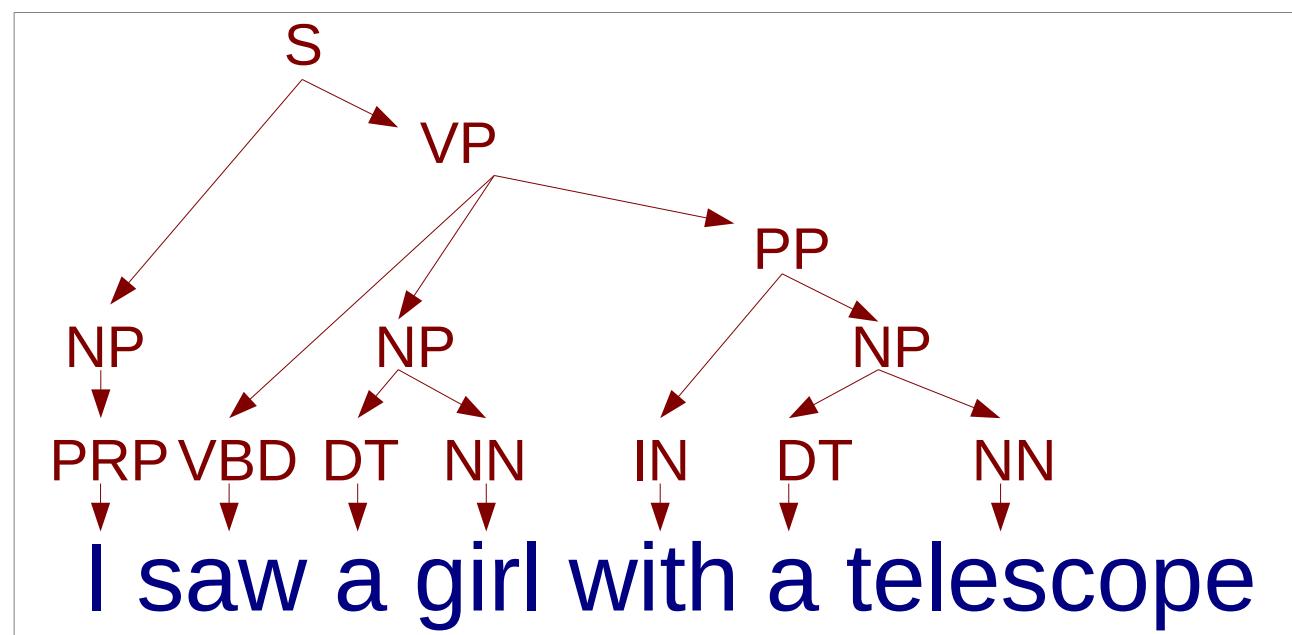
- Given a sentence  $X$ , predict its parse tree  $Y$



- A type of “structured” prediction (similar to POS tagging, word segmentation, etc.)

# Probabilistic Model for Parsing

- Given a sentence  $X$ , predict the most probable parse tree  $Y$



$$\underset{Y}{\operatorname{argmax}} P(Y|X)$$

# Probabilistic Generative Model

- We assume some probabilistic model generated the **parse tree Y** and **sentence X** jointly

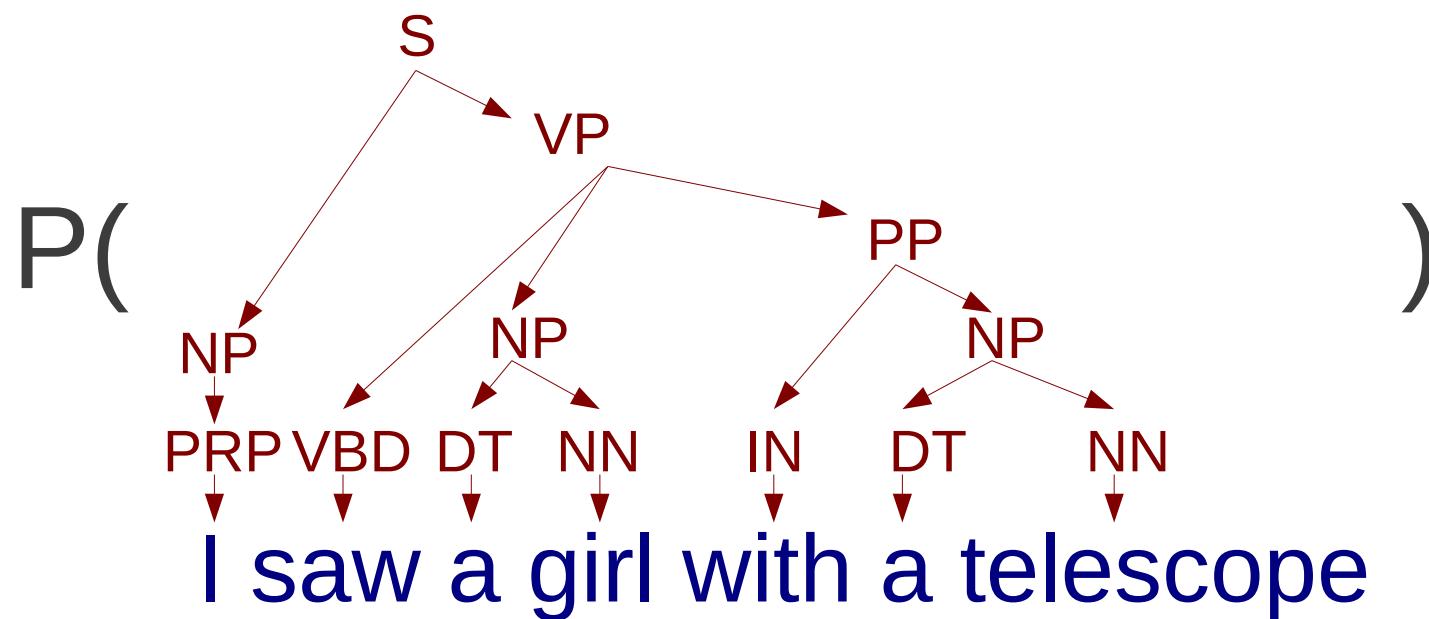
$$P(Y, X)$$

- The parse tree with highest joint probability given X also has the highest conditional probability

$$\underset{Y}{\operatorname{argmax}} P(Y|X) = \underset{Y}{\operatorname{argmax}} P(Y, X)$$

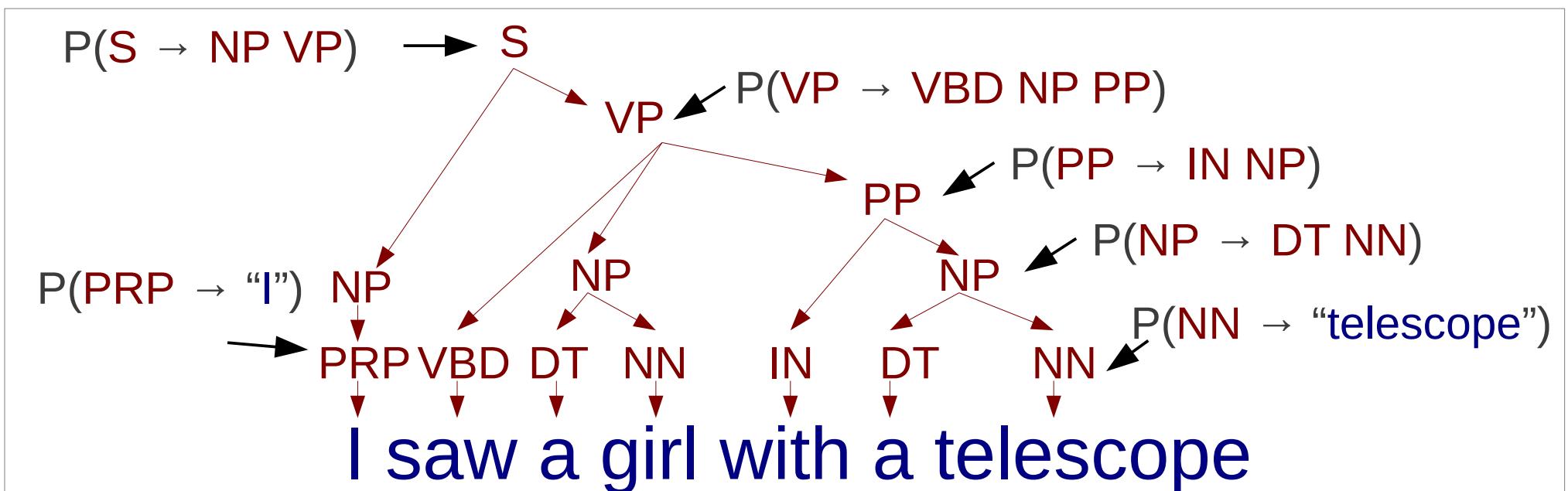
# Probabilistic Context Free Grammar (PCFG)

- How do we define a joint probability for a parse tree?



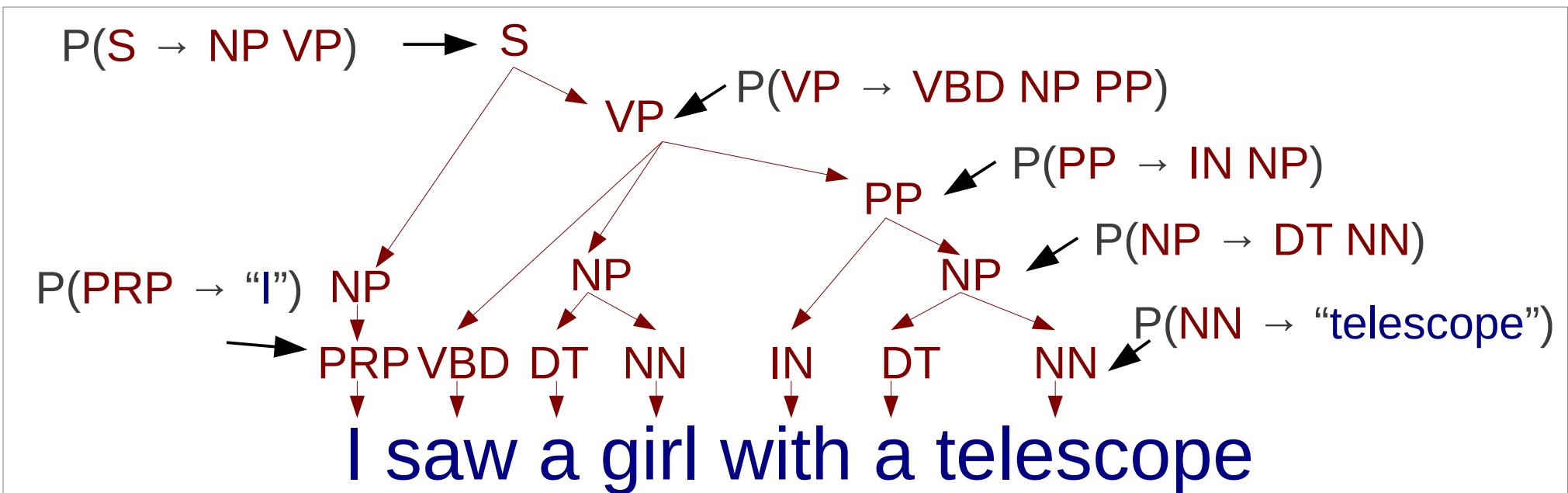
# Probabilistic Context Free Grammar (PCFG)

- PCFG: Define probability for each node



# Probabilistic Context Free Grammar (PCFG)

- PCFG: Define probability for each node



- Parse tree probability is product of node probabilities

$$\begin{aligned} & P(S \rightarrow NP\ VP) * P(NP \rightarrow PRP) * P(PRP \rightarrow "I") \\ & * P(VP \rightarrow VBD\ NP\ PP) * P(VBD \rightarrow "saw") * P(NP \rightarrow DT\ NN) \\ & * P(DT \rightarrow "a") * P(NN \rightarrow "girl") * P(PP \rightarrow IN\ NP) * P(IN \rightarrow "with") \\ & * P(NP \rightarrow DT\ NN) * P(DT \rightarrow "a") * P(NN \rightarrow "telescope") \end{aligned}$$

# Probabilistic Parsing

- Given this model, parsing is the algorithm to find

$$\operatorname{argmax}_Y P(Y, X)$$

- Can we use the Viterbi algorithm as we did before?

# Probabilistic Parsing

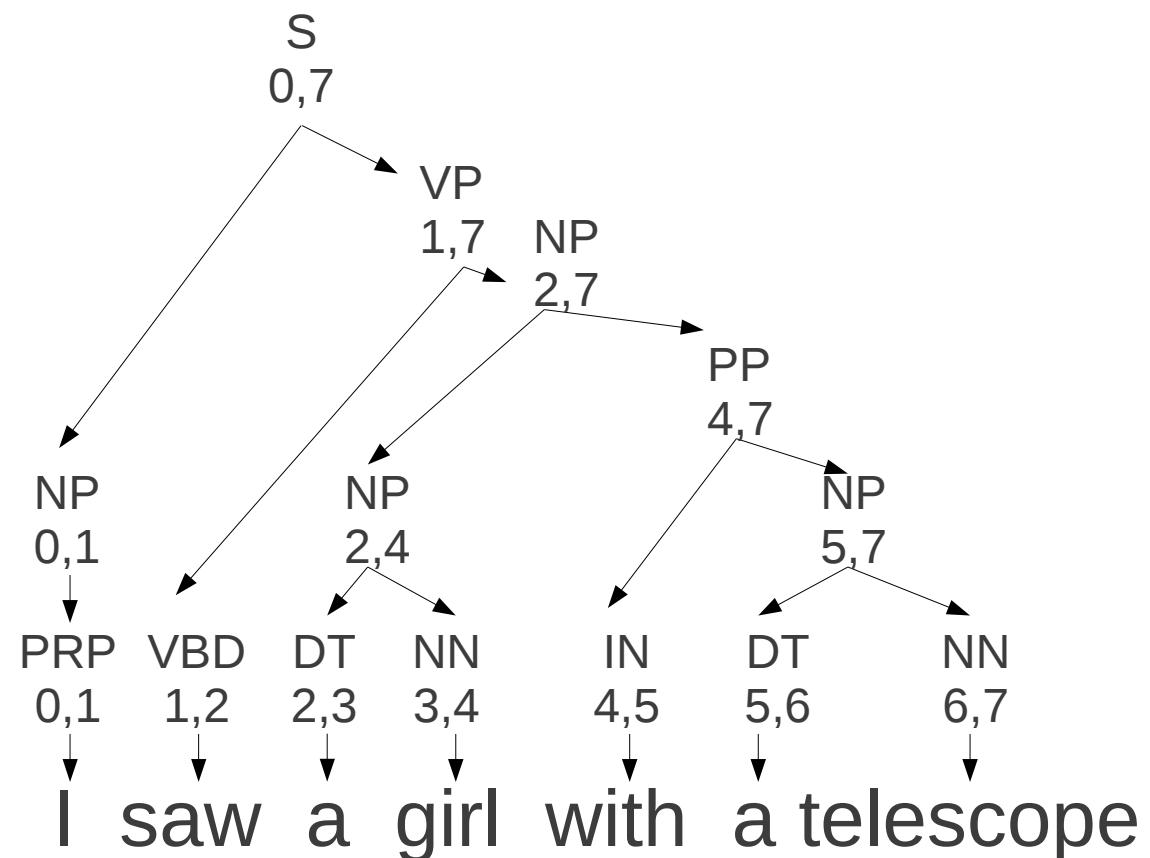
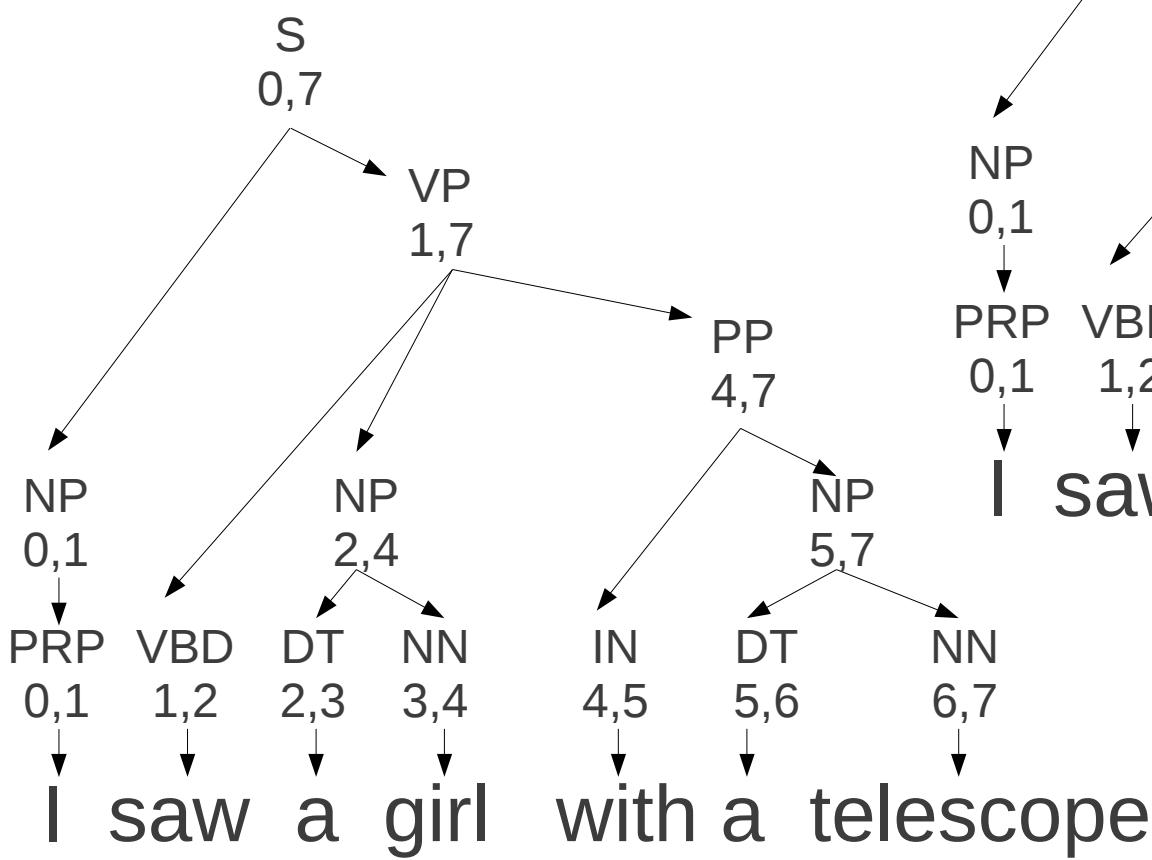
- Given this model, parsing is the algorithm to find

$$\underset{Y}{\operatorname{argmax}} P(Y, X)$$

- Can we use the Viterbi algorithm as we did before?
  - Answer: No!
  - Reason: Parse candidates are not graphs, but hypergraphs.

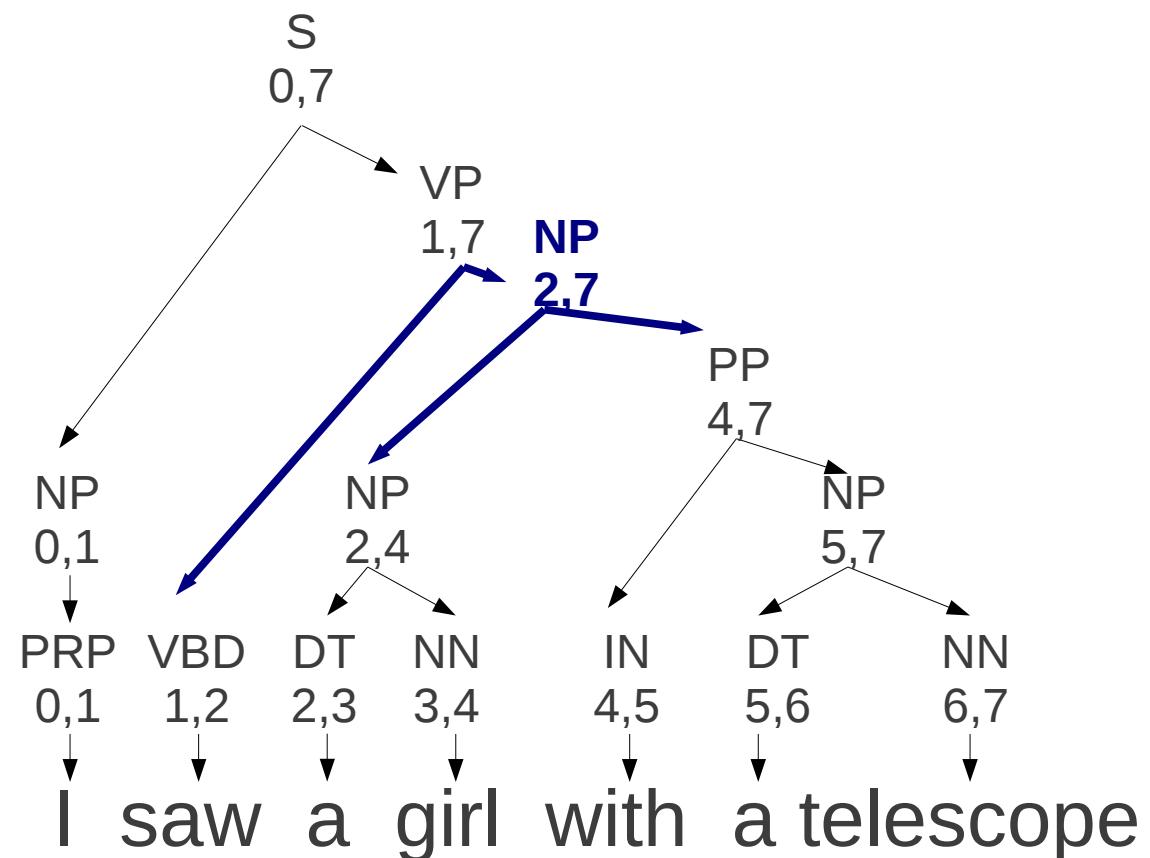
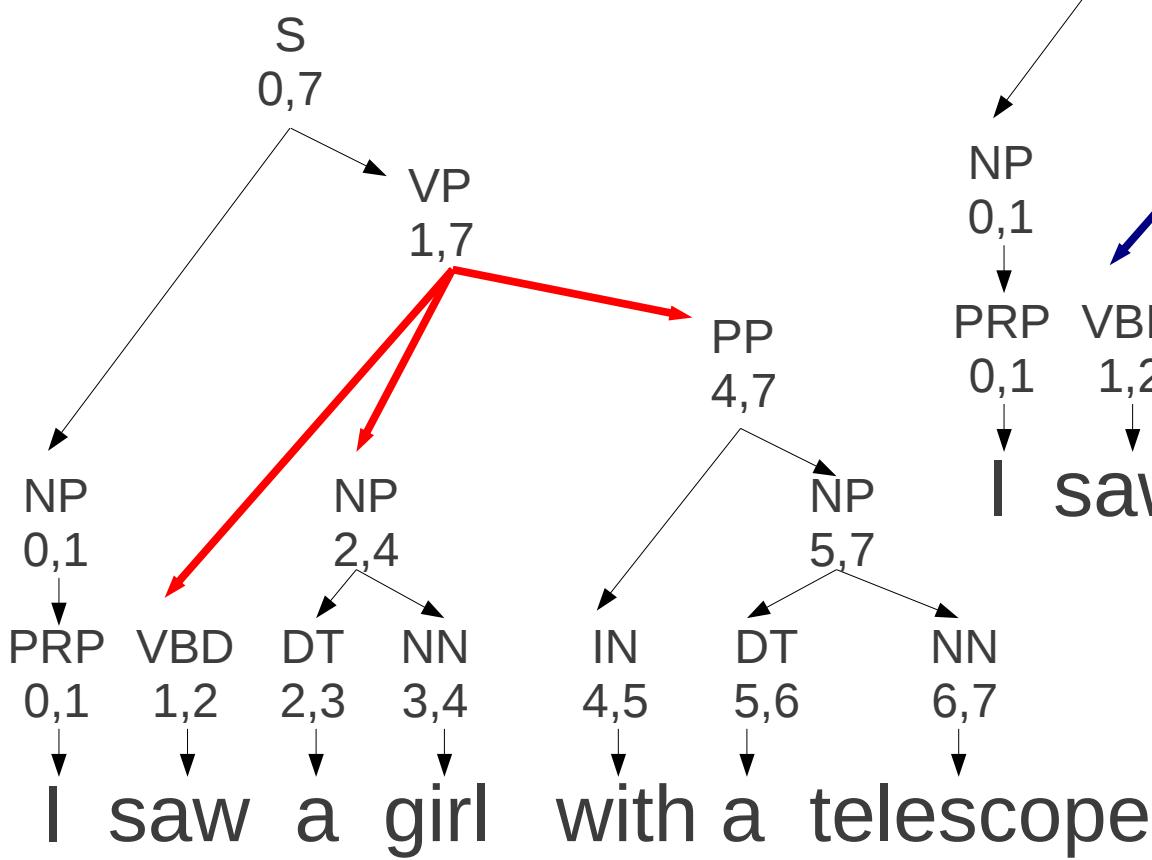
# What is a Hypergraph?

- Let's say we have two parse trees



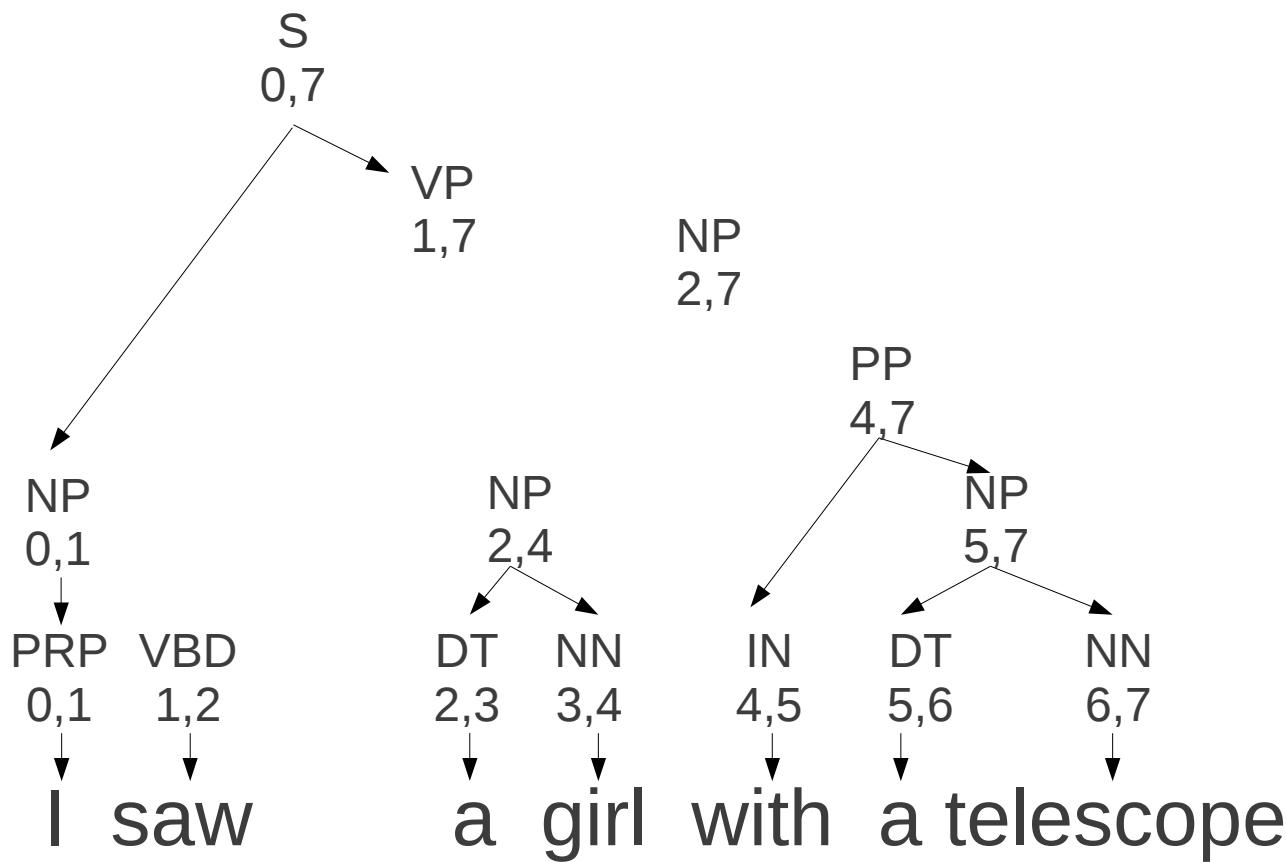
# What is a Hypergraph?

- Most parts are the same!



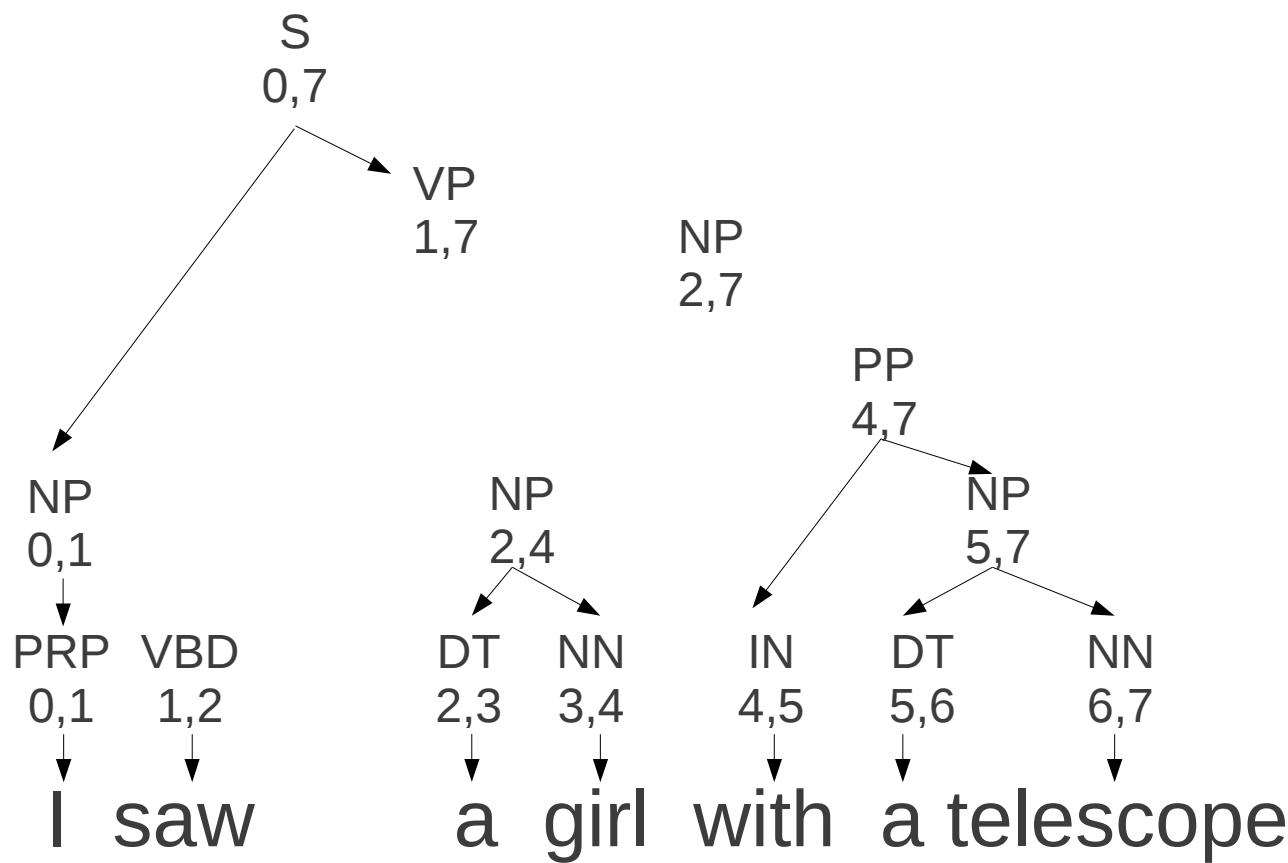
# What is a Hypergraph?

- Graph with all same edges + all nodes



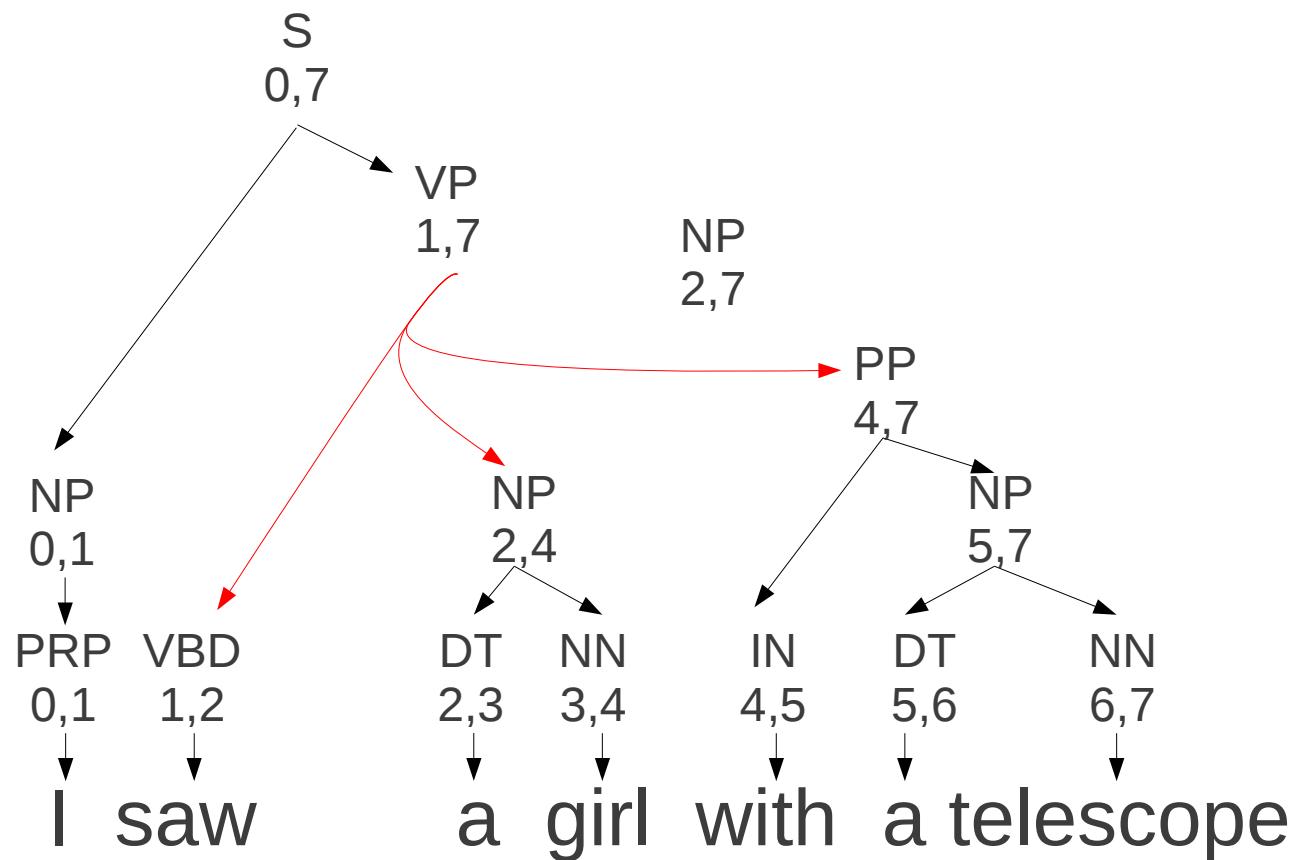
# What is a Hypergraph?

- Create graph with all same edges + all nodes



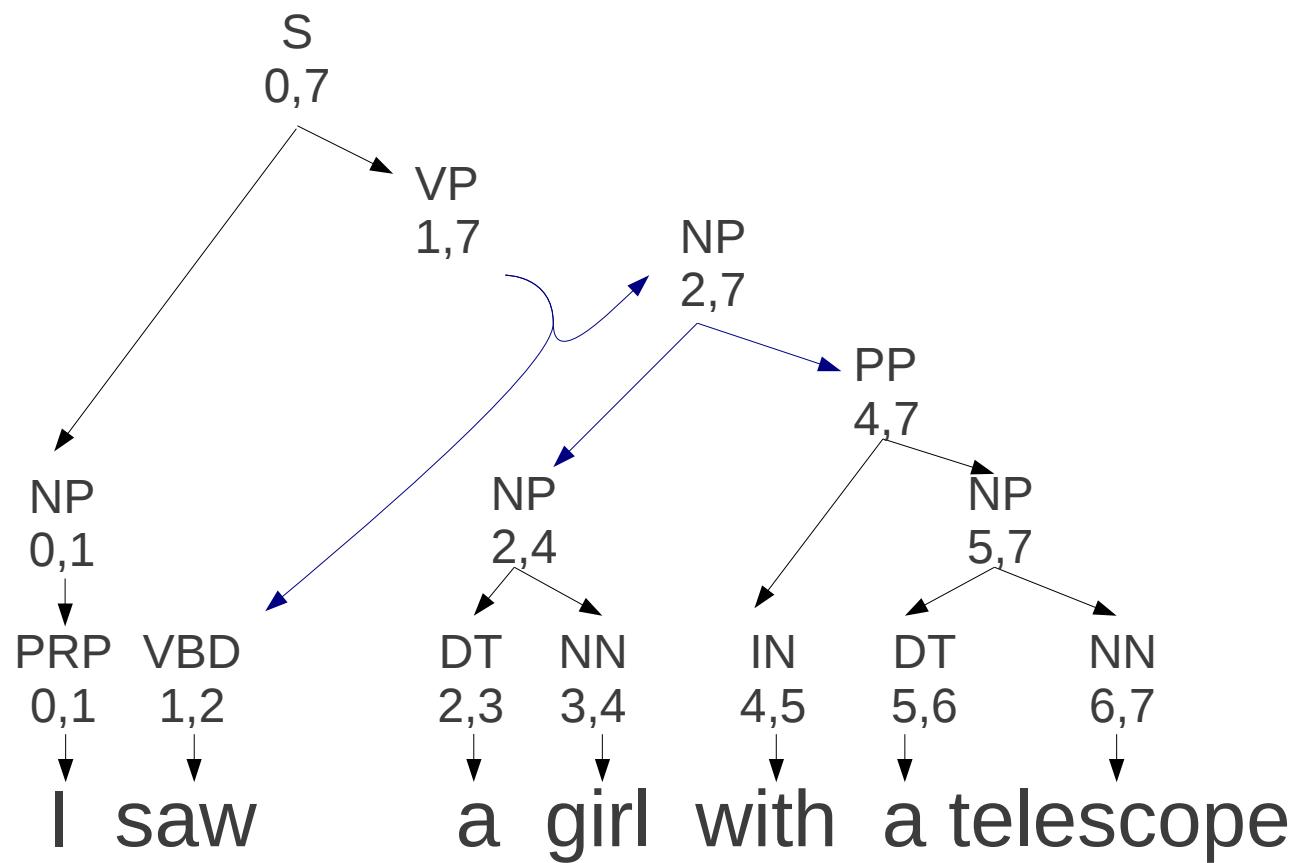
# What is a Hypergraph?

- With the edges in the **first** trees:



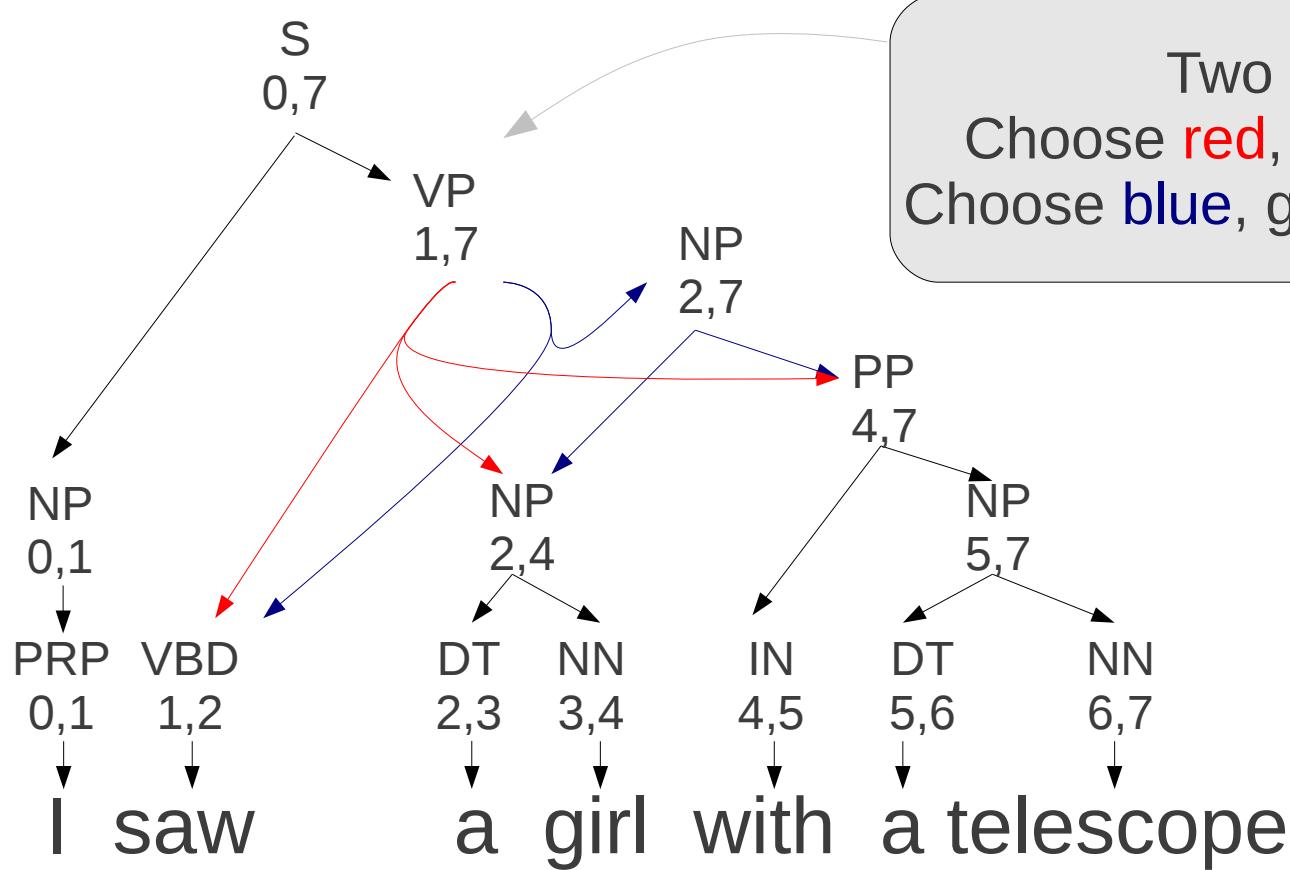
# What is a Hypergraph?

- With the edges in the second tree:



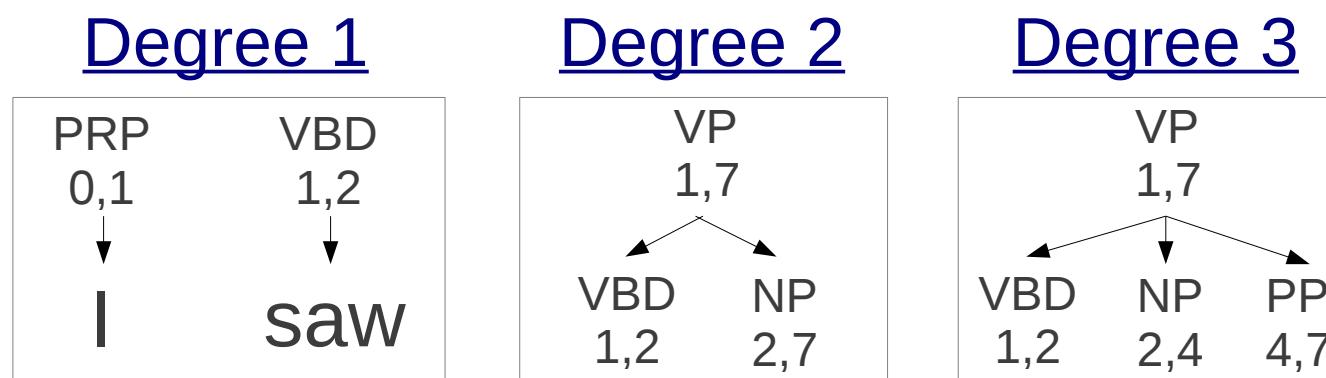
# What is a Hypergraph?

- With the edges in the **first** and **second** trees:



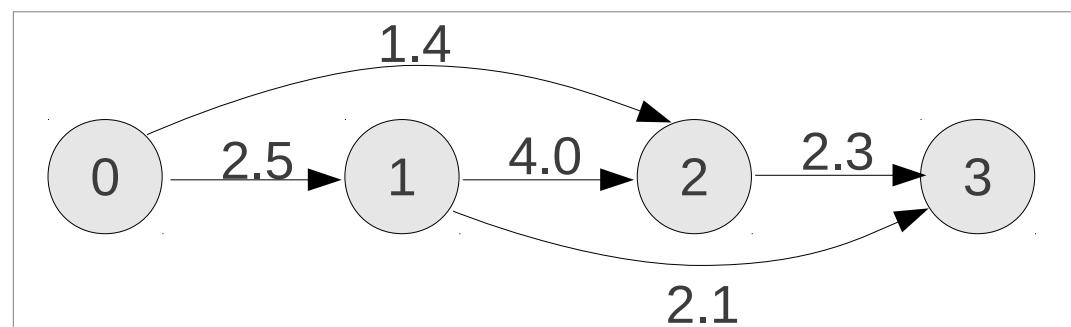
# Why a “Hyper”graph?

- The “degree” of an edge is the number of children



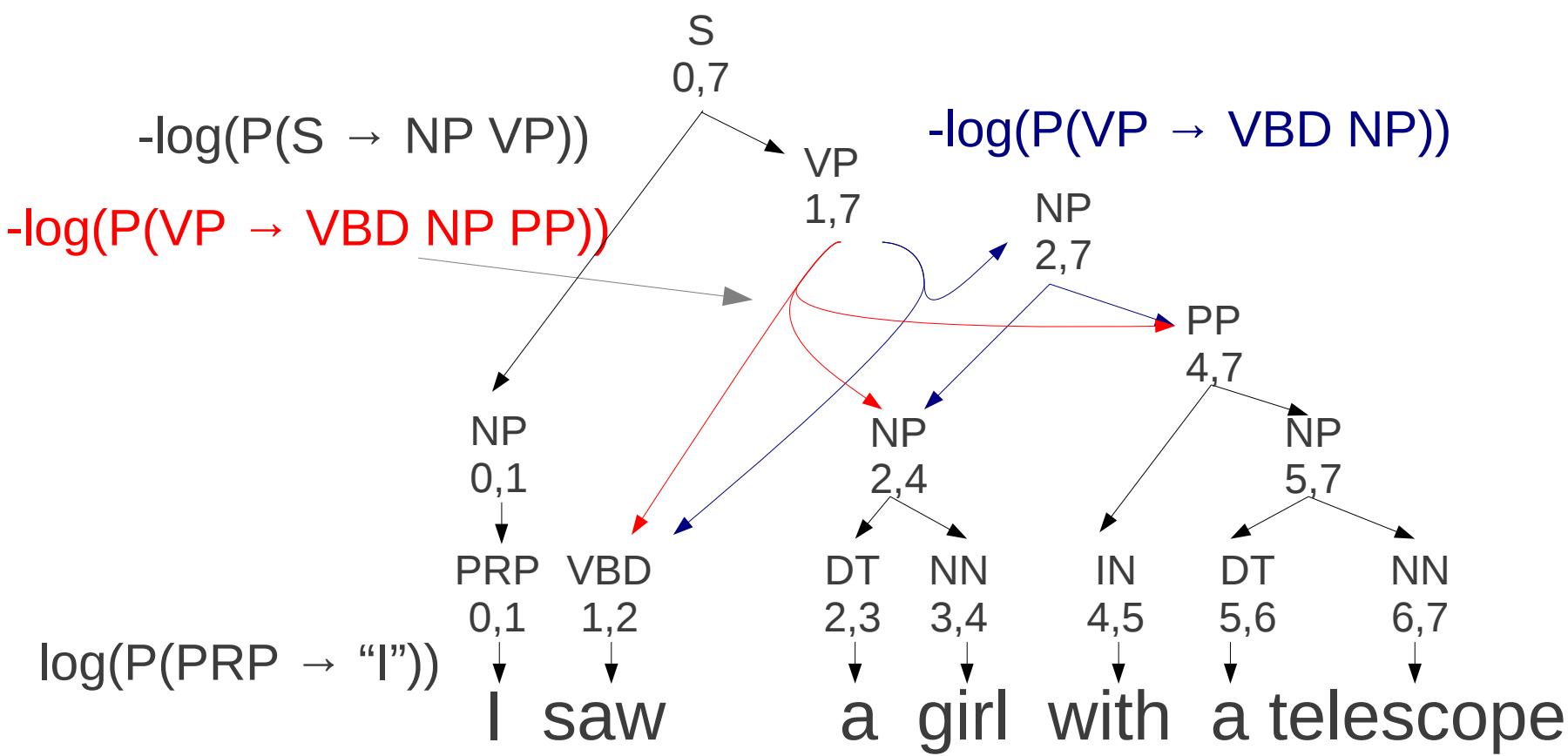
- The degree of a hypergraph is the maximum degree of all its edges
- A graph is a hypergraph of degree 1!

Example →



# Weighted Hypergraphs

- Like graphs:
  - can add weights to hypergraph edges
  - use negative log probability of rule



# Solving Hypergraphs

- Parsing = finding minimum path through a hypergraph

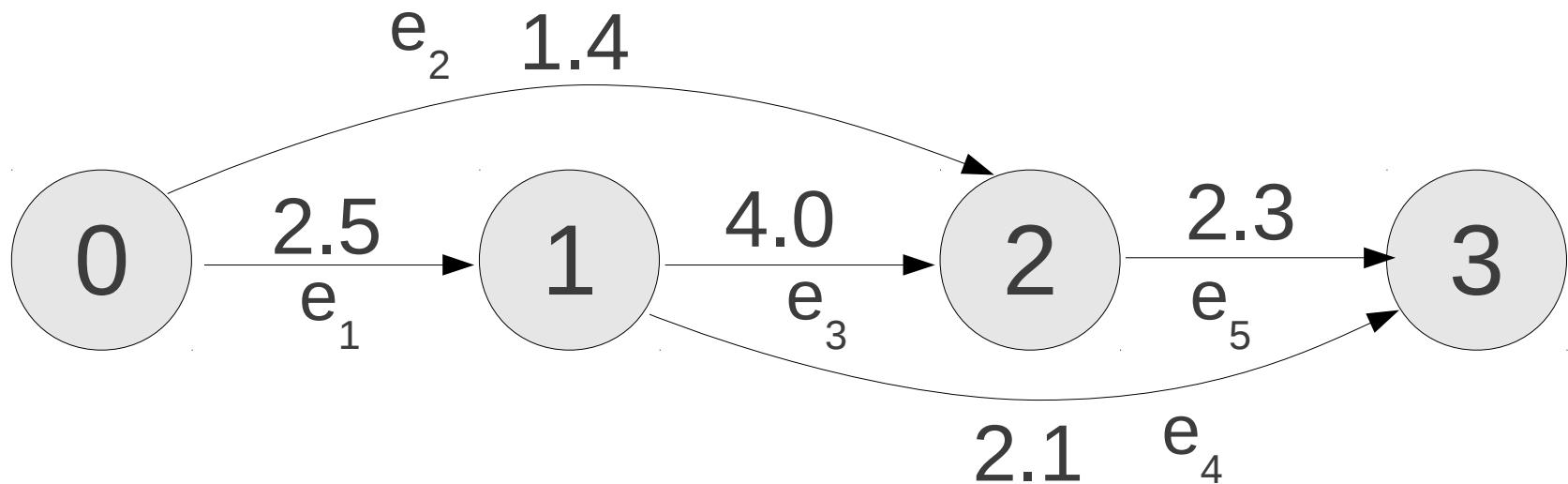
# Solving Hypergraphs

- Parsing = finding minimum path through a hypergraph
- We can do this for graphs with the **Viterbi algorithm**
  - **Forward:** Calculate score of best path to each state
  - **Backward:** Recover the best path

# Solving Hypergraphs

- Parsing = finding minimum path through a hypergraph
- We can do this for graphs with the **Viterbi algorithm**
  - **Forward:** Calculate score of best path to each state
  - **Backward:** Recover the best path
- For hypergraphs, almost identical algorithm!
  - **Inside:** Calculate score of best subtree for each node
  - **Outside:** Recover the best tree

# Review: Viterbi Algorithm (Forward Step)



`best_score[0] = 0`

**for each** *node* in the *graph* (ascending order)

`best_score[node] = ∞`

**for each** incoming edge of *node*

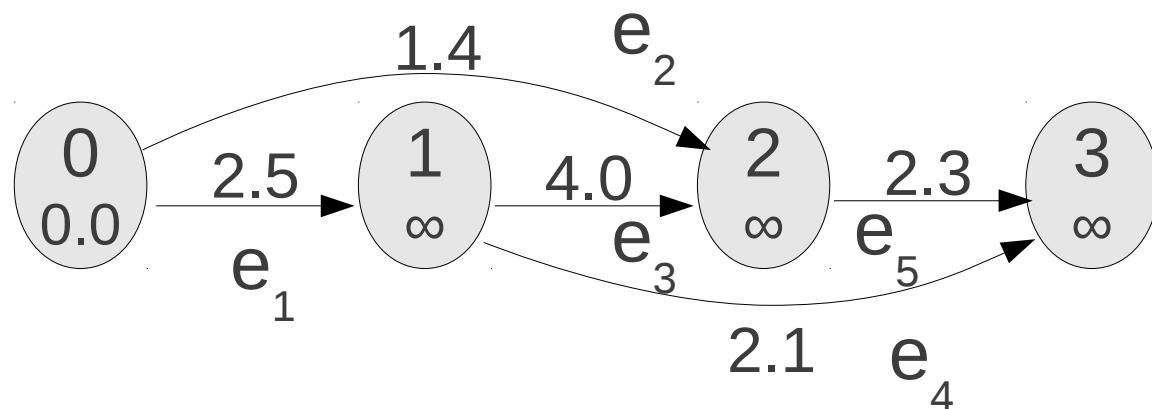
`score = best_score[edge.prev_node] + edge.score`

**if** `score < best_score[node]`

`best_score[node] = score`

`best_edge[node] = edge`

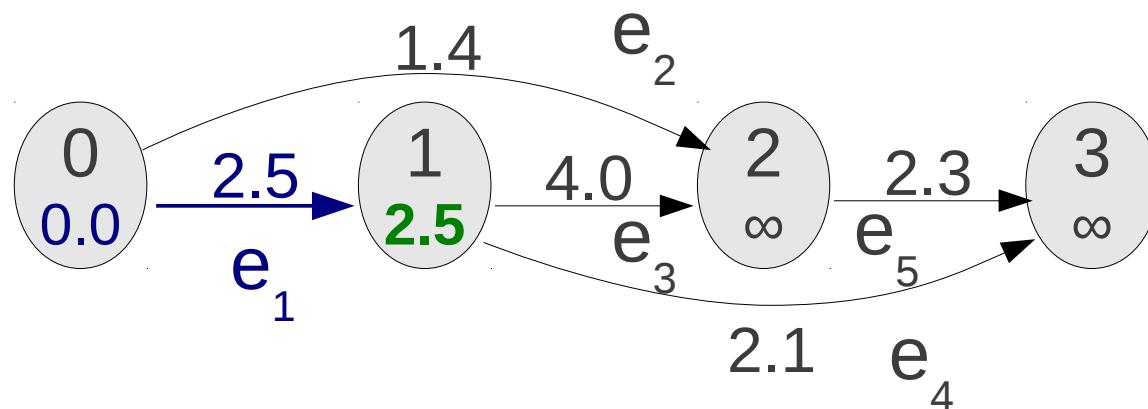
# Example:



Initialize:

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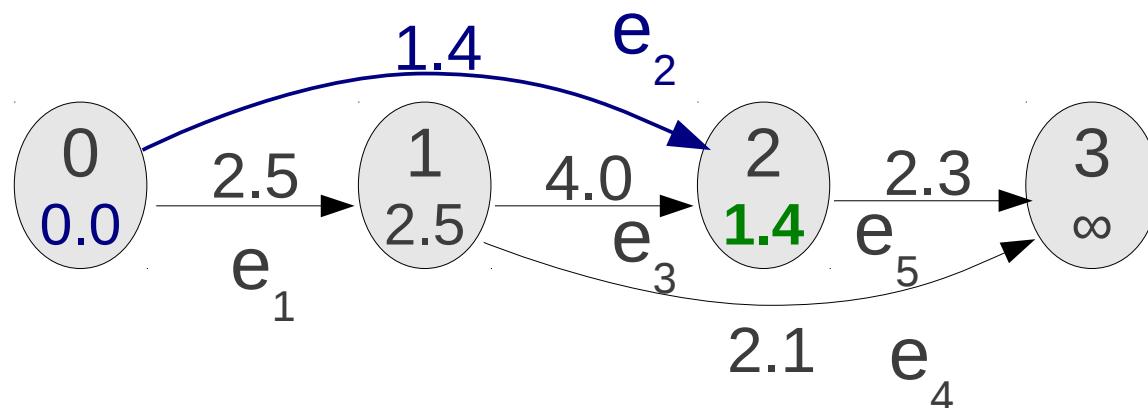
Check  $e_1$ :

$\text{score} = 0 + 2.5 = 2.5 (< \infty)$

`best_score[1] = 2.5`

`best_edge[1] =  $e_1$`

# Example:



Initialize:

`best_score[0] = 0`

Check  $e_1$ :

$\text{score} = 0 + 2.5 = 2.5 (< \infty)$

`best_score[1] = 2.5`

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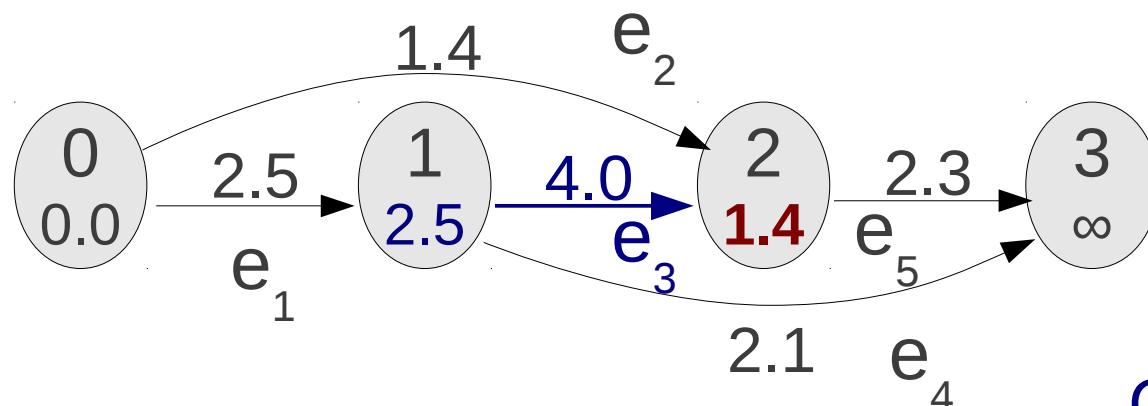
Check  $e_2$ :

$\text{score} = 0 + 1.4 = 1.4 (< \infty)$

`best_score[2] = 1.4`

`best_edge[2] =  $e_2$`

# Example:



Initialize:

best\_score[0] = 0

Check  $e_1$ :

score =  $0 + 2.5 = 2.5 (< \infty)$

best\_score[1] = 2.5

best\_edge[1] =  $e_1$

Check  $e_2$ :

score =  $0 + 1.4 = 1.4 (< \infty)$

best\_score[2] = 1.4

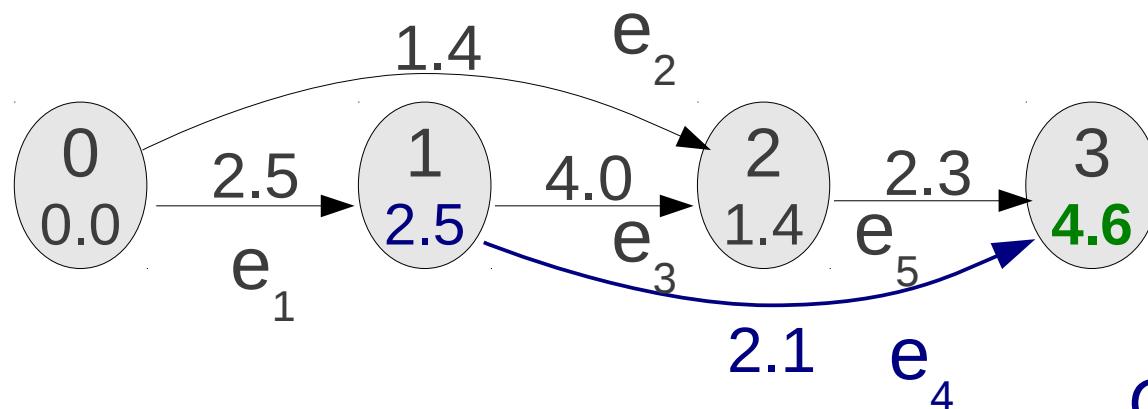
best\_edge[2] =  $e_2$

Check  $e_3$ :

score =  $2.5 + 4.0 = 6.5 (> 1.4)$

No change!

# Example:



Initialize:

```
best_score[0] = 0
```

Check  $e_1$ :

score =  $0 + 2.5 = 2.5 (< \infty)$

```
best_score[1] = 2.5
```

```
best_edge[1] =  $e_1$ 
```

Check  $e_2$ :

score =  $0 + 1.4 = 1.4 (< \infty)$

```
best_score[2] = 1.4
```

```
best_edge[2] =  $e_2$ 
```

Check  $e_3$ :

score =  $2.5 + 4.0 = 6.5 (> 1.4)$

No change!

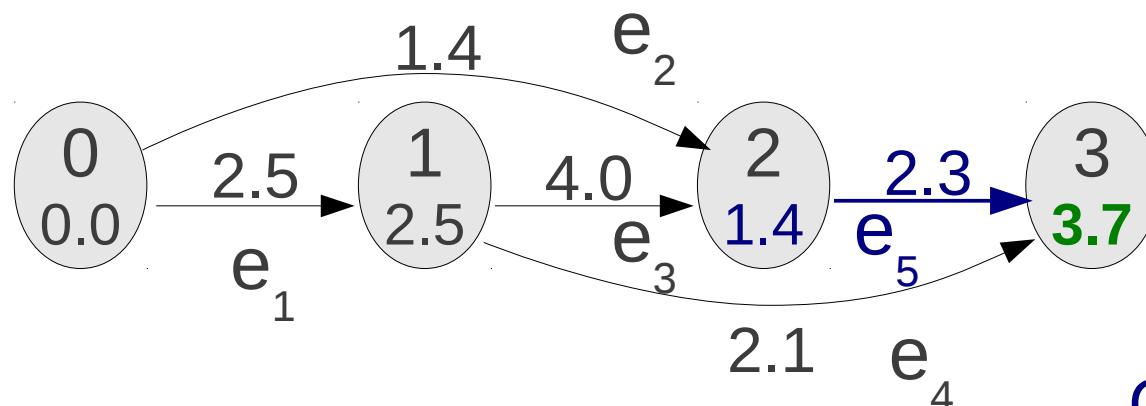
Check  $e_4$ :

score =  $2.5 + 2.1 = 4.6 (< \infty)$

```
best_score[3] = 4.6
```

```
best_edge[3] =  $e_4$ 
```

# Example:



Initialize:

best\_score[0] = 0

Check  $e_1$ :

score =  $0 + 2.5 = 2.5 (< \infty)$

best\_score[1] = 2.5

best\_edge[1] =  $e_1$

Check  $e_2$ :

score =  $0 + 1.4 = 1.4 (< \infty)$

best\_score[2] = 1.4

best\_edge[2] =  $e_2$

Check  $e_3$ :

score =  $2.5 + 4.0 = 6.5 (> 1.4)$

No change!

Check  $e_4$ :

score =  $2.5 + 2.1 = 4.6 (< \infty)$

~~best\_score[3] = 4.6~~

~~best\_edge[3] =  $e_4$~~

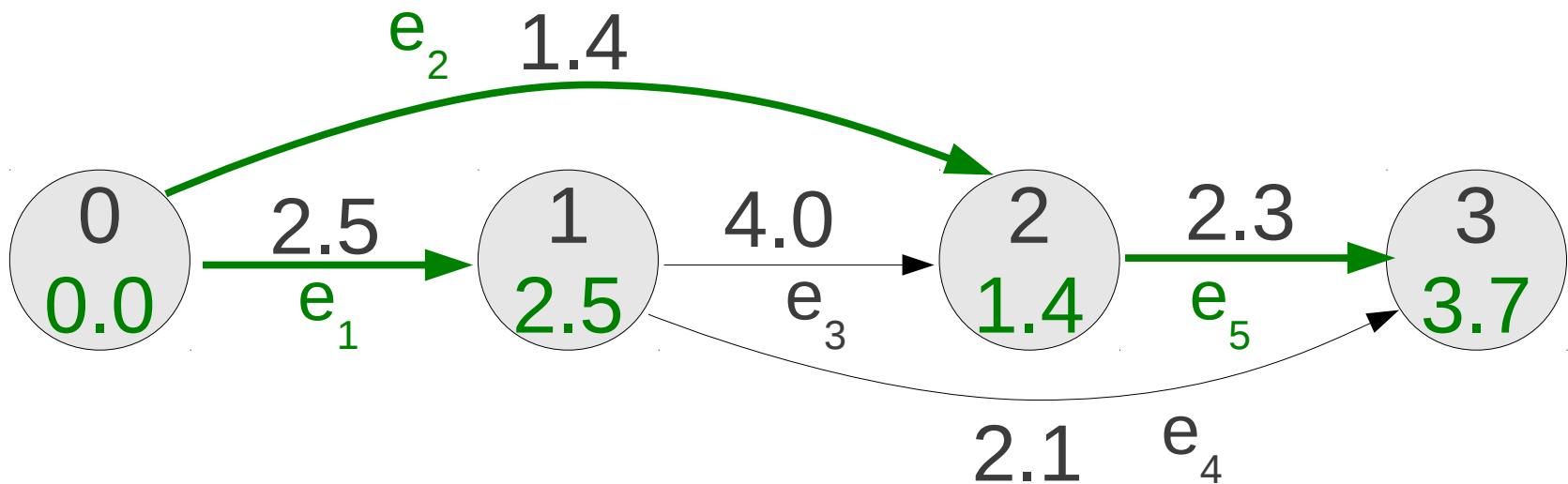
Check  $e_5$ :

score =  $1.4 + 2.3 = 3.7 (< 4.6)$

best\_score[3] = 3.7

best\_edge[3] =  $e_5$

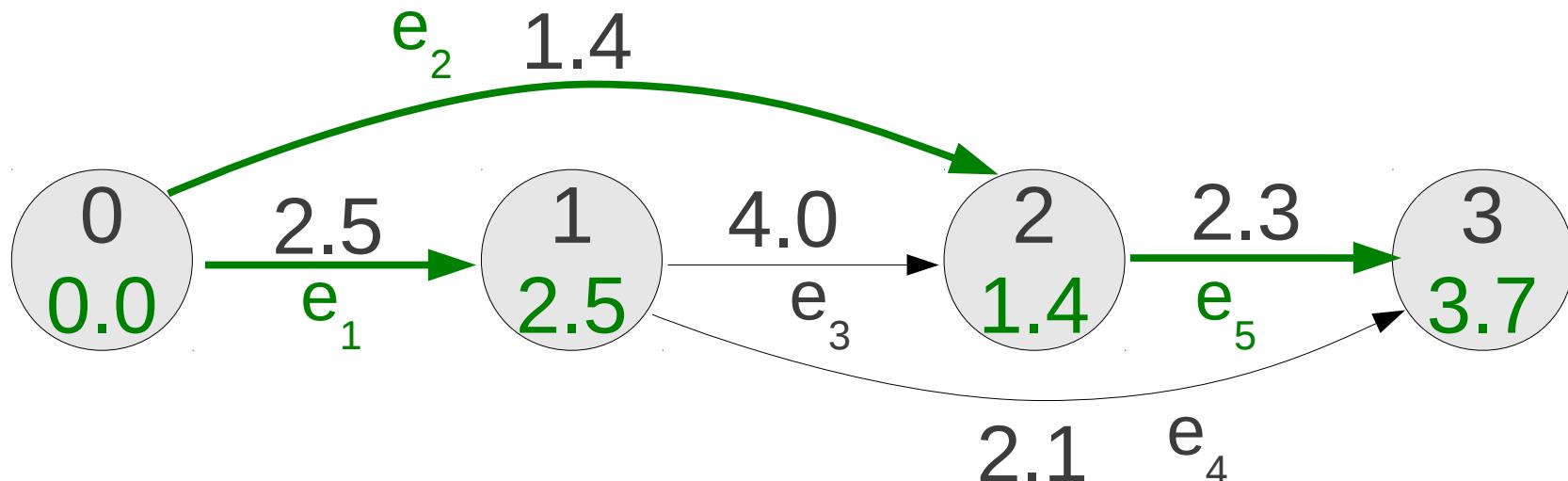
# Result of Forward Step



*best\_score = ( 0.0, 2.5, 1.4, 3.7 )*

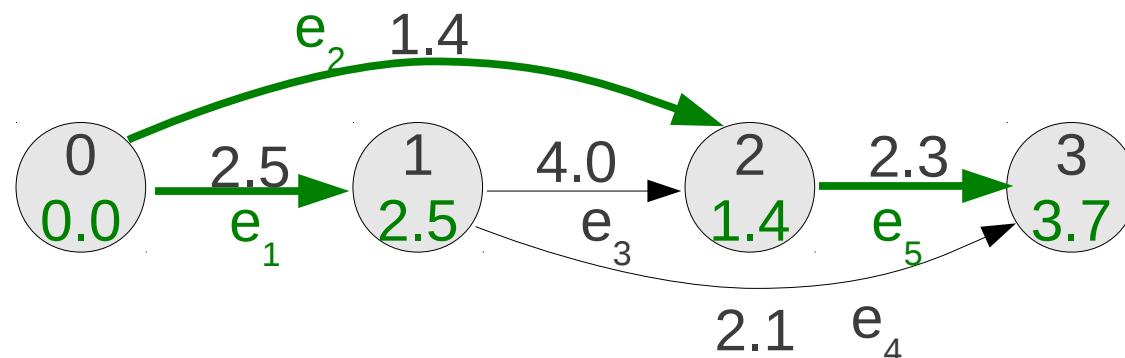
*best\_edge = ( NULL,  $e_1$ ,  $e_2$ ,  $e_5$  )*

# Review: Viterbi Algorithm (Backward Step)



```
best_path = []
next_edge = best_edge[best_edge.length - 1]
while next_edge != NULL
    add next_edge to best_path
    next_edge = best_edge[next_edge.prev_node]
reverse best_path
```

# Example of Backward Step

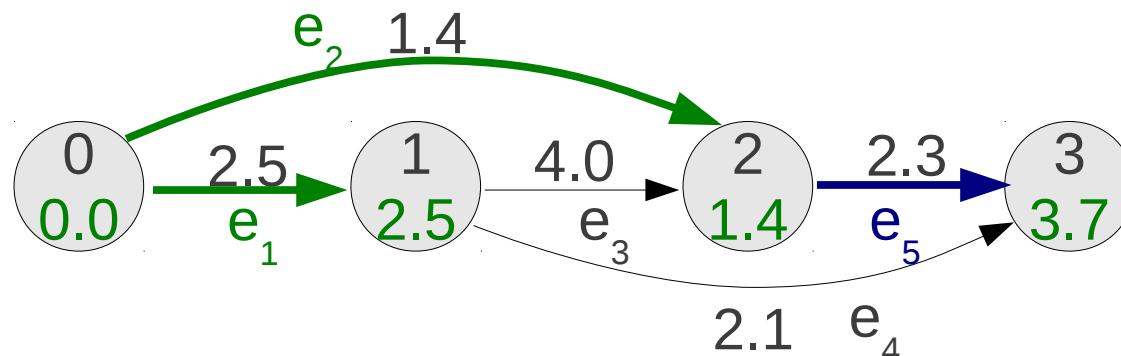


Initialize:

```
best_path = []
```

```
next_edge = best_edge[3] = e5
```

# Example of Backward Step



Initialize:

```
best_path = []
```

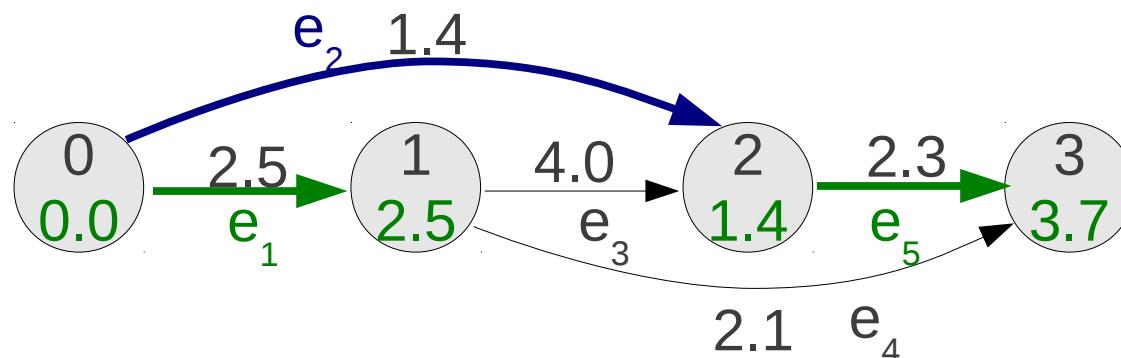
```
next_edge = best_edge[3] = e5
```

Process  $e_5$ :

```
best_path = [e5]
```

```
next_edge = best_edge[2] = e2
```

# Example of Backward Step



Initialize:

```
best_path = []
next_edge = best_edge[3] = e5
```

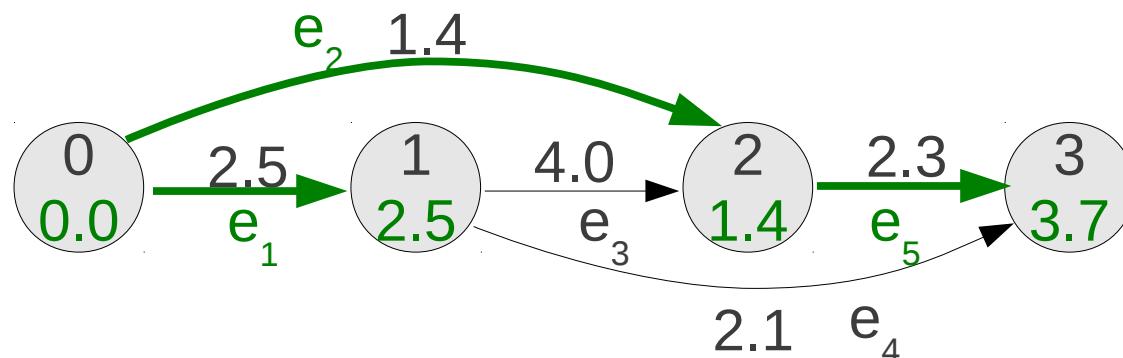
Process  $e_2$ :

```
best_path = [e5, e2]
next_edge = best_edge[0] = NULL
```

Process  $e_5$ :

```
best_path = [e5]
next_edge = best_edge[2] = e2
```

# Example of Backward Step



## Initialize:

```
best_path = []
next_edge = best_edge[3] = e5
```

## Process $e_5$ :

```
best_path = [e5]
next_edge = best_edge[2] = e2
```

## Process $e_5$ :

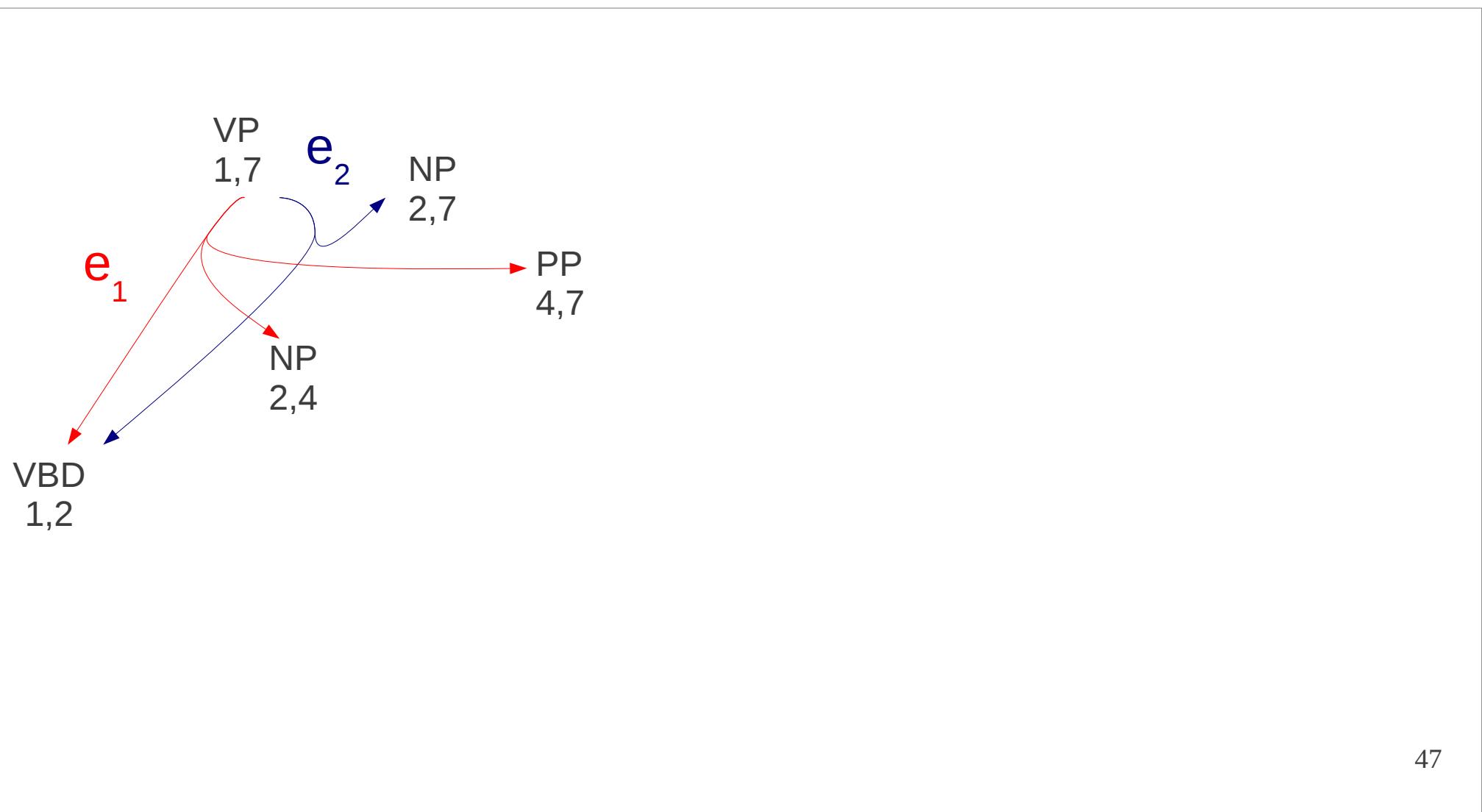
```
best_path = [e5, e2]
next_edge = best_edge[0] = NULL
```

## Reverse:

```
best_path = [e2, e5]
```

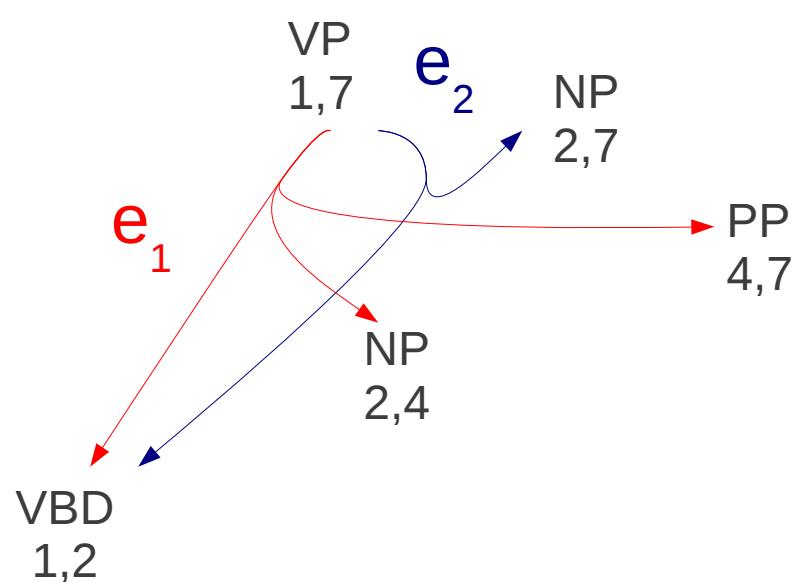
# Inside Step for Hypergraphs:

- Find the score of best subtree of VP1,7



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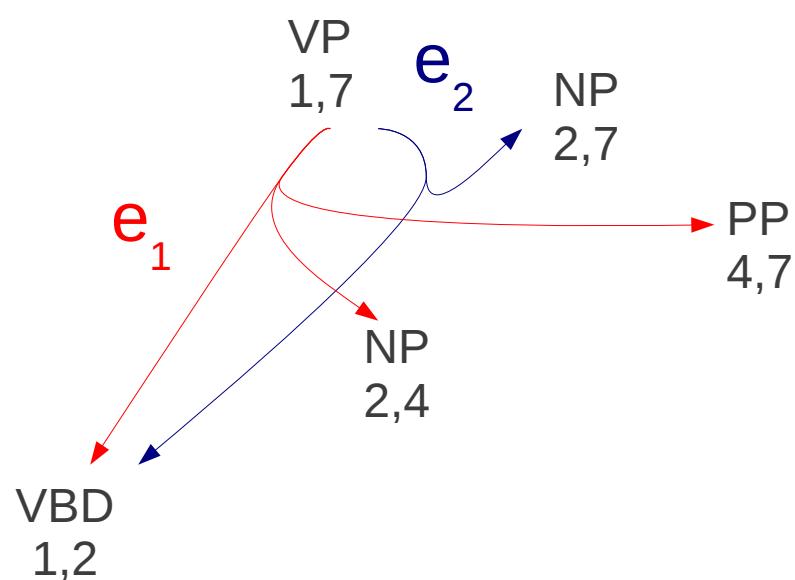


$$\begin{aligned} \text{score}(e_1) = & -\log(P(\text{VP} \rightarrow \text{VBD } \text{NP } \text{PP})) + \\ & \text{best\_score}[\text{VBD}1,2] + \\ & \text{best\_score}[\text{NP}2,4] + \\ & \text{best\_score}[\text{NP}2,7] \end{aligned}$$

$$\begin{aligned} \text{score}(e_2) = & -\log(P(\text{VP} \rightarrow \text{VBD } \text{NP})) + \\ & \text{best\_score}[\text{VBD}1,2] + \\ & \text{best\_score}[\text{VBD}2,7] \end{aligned}$$

# Inside Step for Hypergraphs:

- Find the score of best subtree of VP1,7



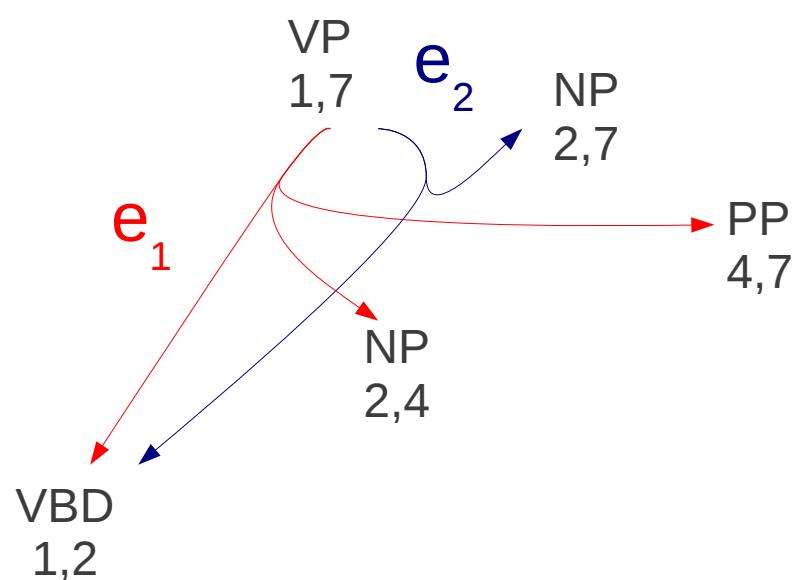
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$$\text{best\_edge}[\text{VB}1,7] = \operatorname{argmin}_{e1,e2} \text{score}$$

# Inside Step for Hypergraphs:

- Find the score of best subtree of VP1,7



$$\begin{aligned} \text{score}(e_1) = & -\log(P(\text{VP} \rightarrow \text{VBD NP PP})) + \\ & \text{best\_score}[\text{VBD1,2}] + \\ & \text{best\_score}[\text{NP2,4}] + \\ & \text{best\_score}[\text{NP2,7}] \end{aligned}$$

$$\begin{aligned} \text{score}(e_2) = & -\log(P(\text{VP} \rightarrow \text{VBD NP})) + \\ & \text{best\_score}[\text{VBD1,2}] + \\ & \text{best\_score}[\text{VBD2,7}] \end{aligned}$$

$$\begin{aligned} \text{best\_edge}[\text{VB1,7}] &= \operatorname{argmin}_{e1,e2} \text{score} \\ \text{best\_score}[\text{VB1,7}] &= \\ &\text{score}(\text{best\_edge}[\text{VB1,7}]) \end{aligned}$$

# Building Hypergraphs from Grammars

- Ok, we can solve hypergraphs, but what we have is:

## A Grammar

$P(S \rightarrow NP VP) = 0.8$

$P(S \rightarrow PRP VP) = 0.2$

$P(VP \rightarrow VBD NP PP) = 0.6$

$P(VP \rightarrow VBD NP) = 0.4$

$P(NP \rightarrow DT NN) = 0.5$

$P(NP \rightarrow NN) = 0.5$

$P(PRP \rightarrow "I") = 0.4$

$P(VBD \rightarrow "saw") = 0.05$

$P(DT \rightarrow "a") = 0.6$

...

## A Sentence

I saw a girl with a telescope

- How do we build a hypergraph?

# CKY Algorithm

- The CKY (Cocke-Kasami-Younger) algorithm creates and solves hypergraphs
- Grammar must be in Chomsky normal form (CNF)
  - All rules have two non-terminals or one terminal on right

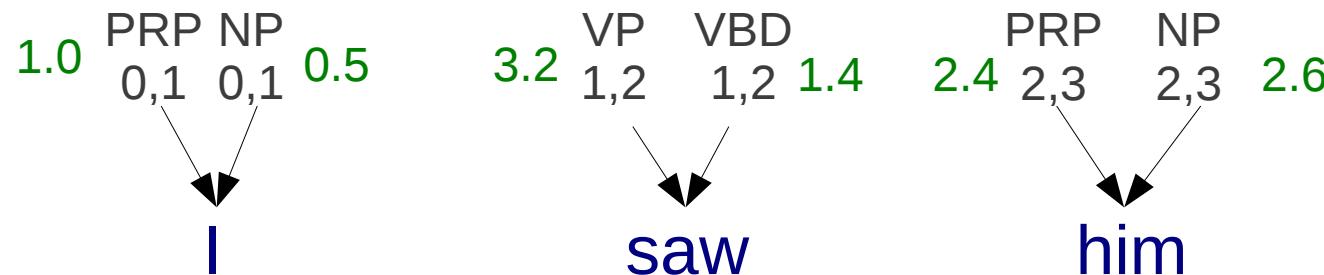
<u>OK</u>	<u>OK</u>	<u>Not OK!</u>
$S \rightarrow NP VP$	$PRP \rightarrow "I"$	$VP \rightarrow VBD NP PP$
$S \rightarrow PRP VP$	$VBD \rightarrow "saw"$	$NP \rightarrow NN$
$VP \rightarrow VBD NP$	$DT \rightarrow "a"$	$NP \rightarrow PRP$

- Can convert rules into CNF

$VP \rightarrow VBD NP PP$	$\rightarrow$	$VP \rightarrow VBD VP'$
		$VP' \rightarrow NP PP$
$NP \rightarrow PRP + PRP \rightarrow "I"$	$\rightarrow$	$NP\_PRP \rightarrow "I"$

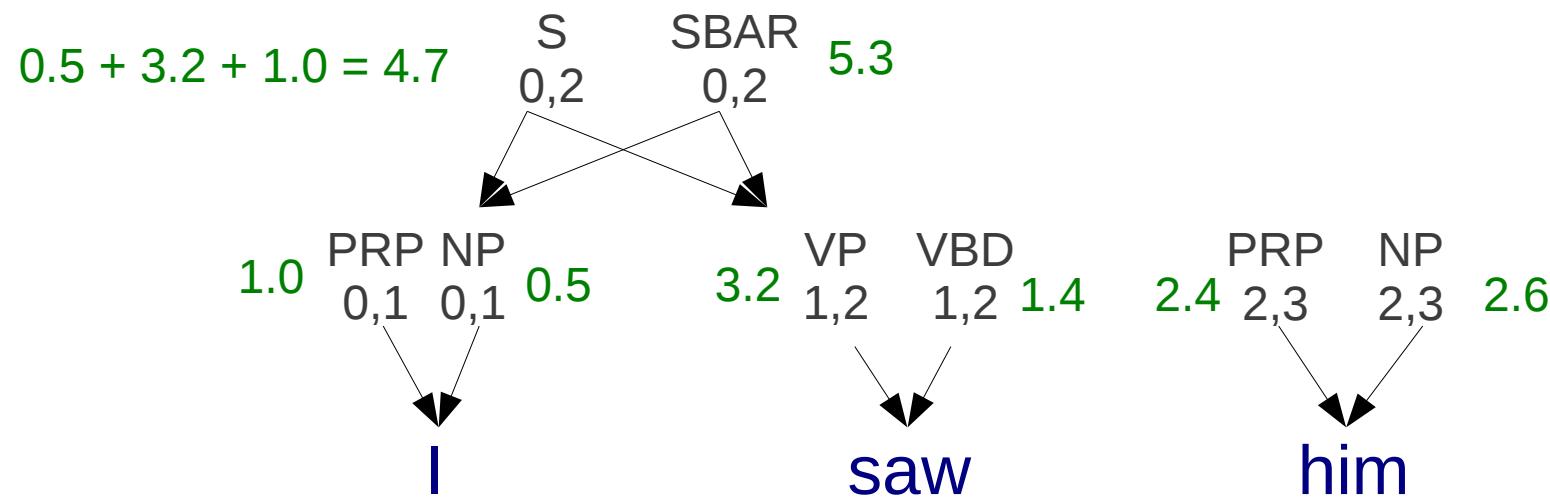
# CKY Algorithm

- Start by expanding all rules for terminals with **scores**



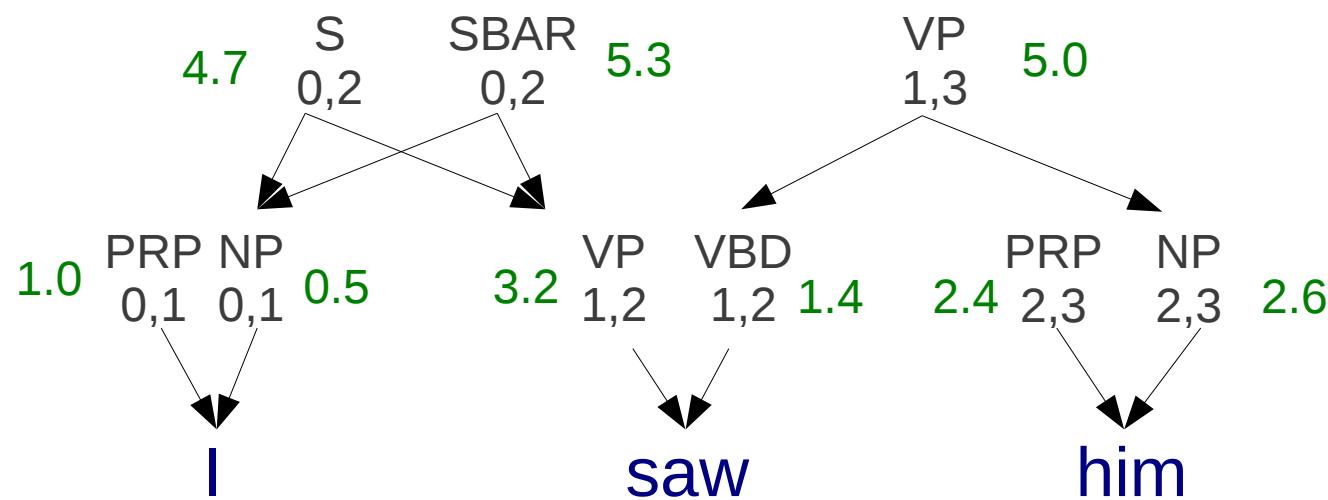
# CKY Algorithm

- Expand all possible nodes for 0,2



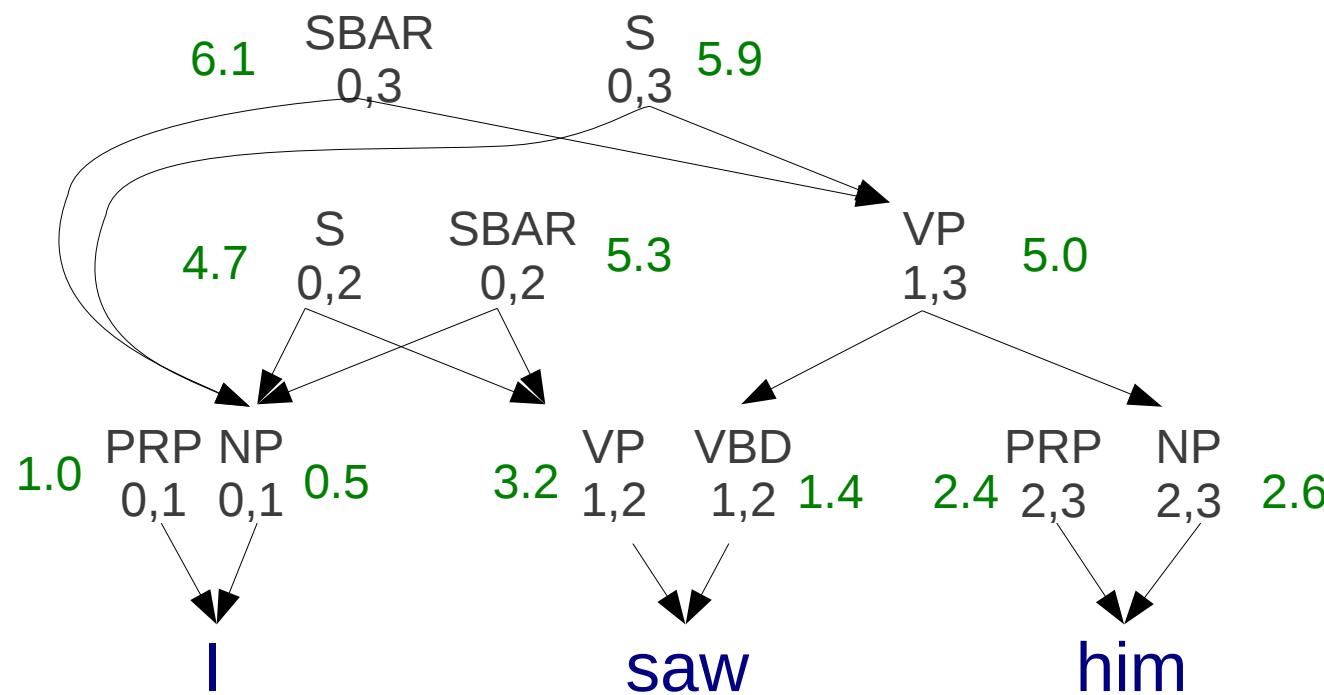
# CKY Algorithm

- Expand all possible nodes for 1,3



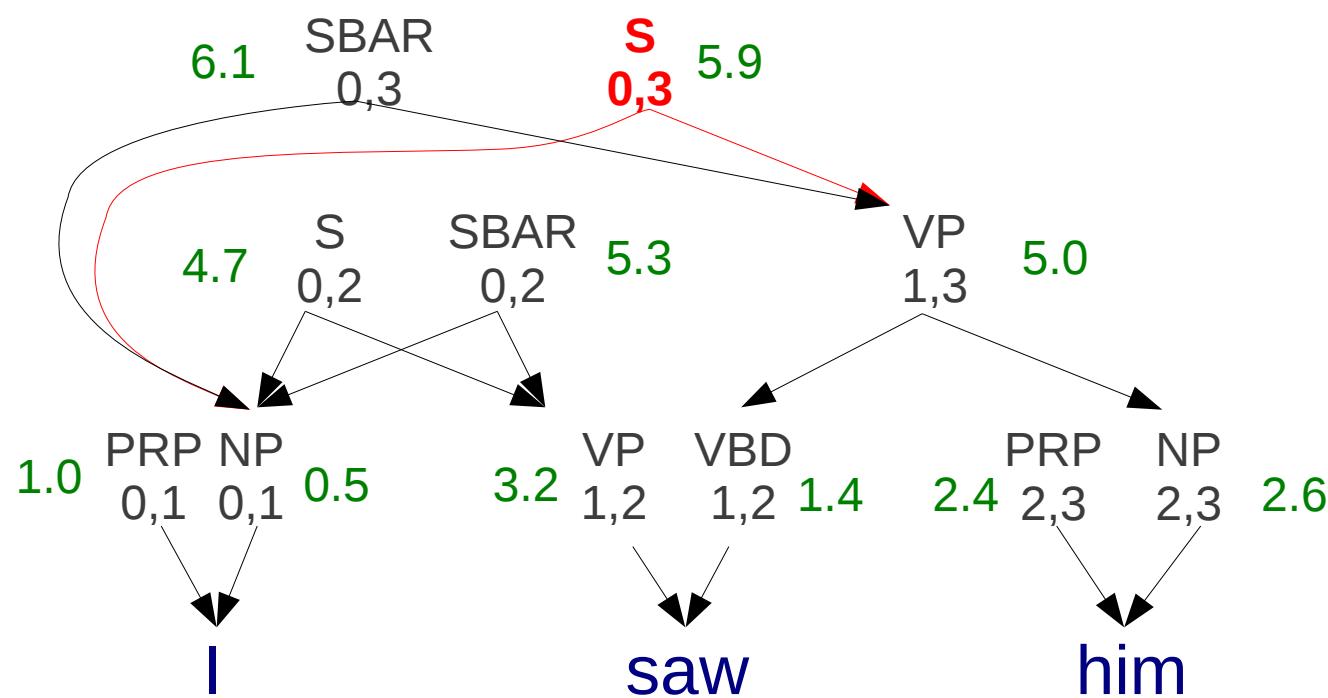
# CKY Algorithm

- Expand all possible nodes for 0,3



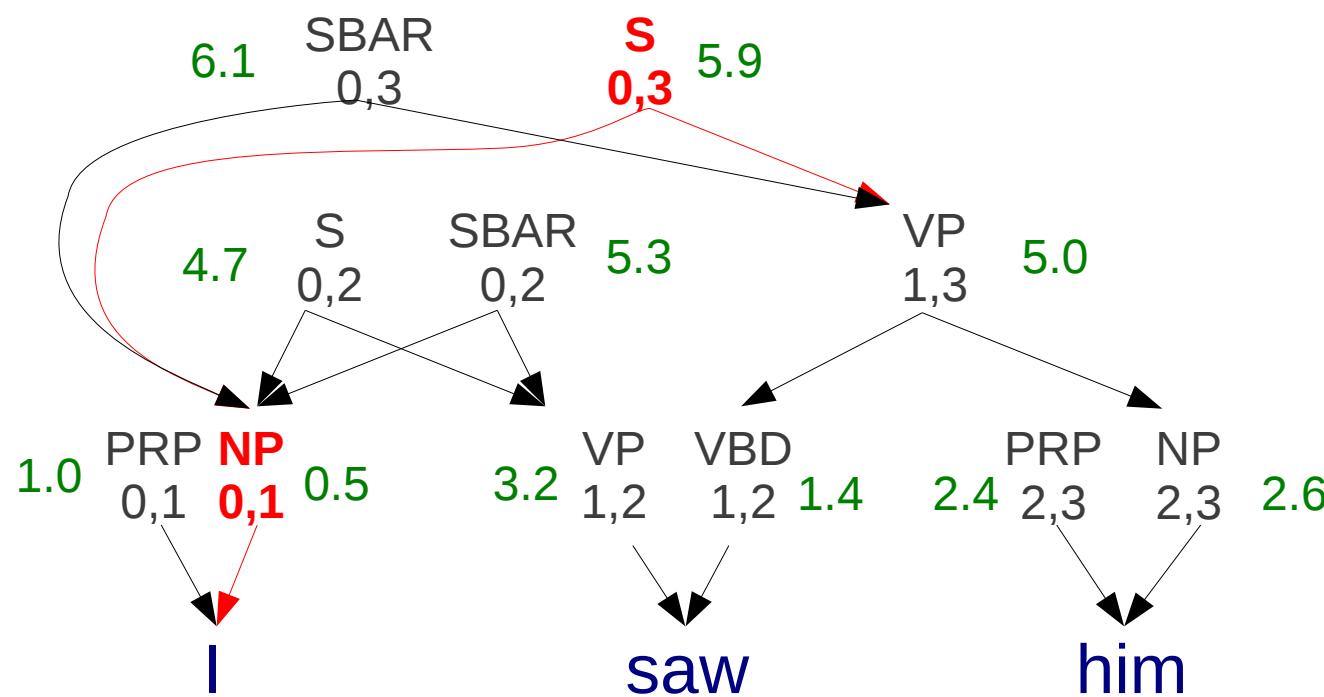
# CKY Algorithm

- Find the S that covers the entire sentence and its best edge



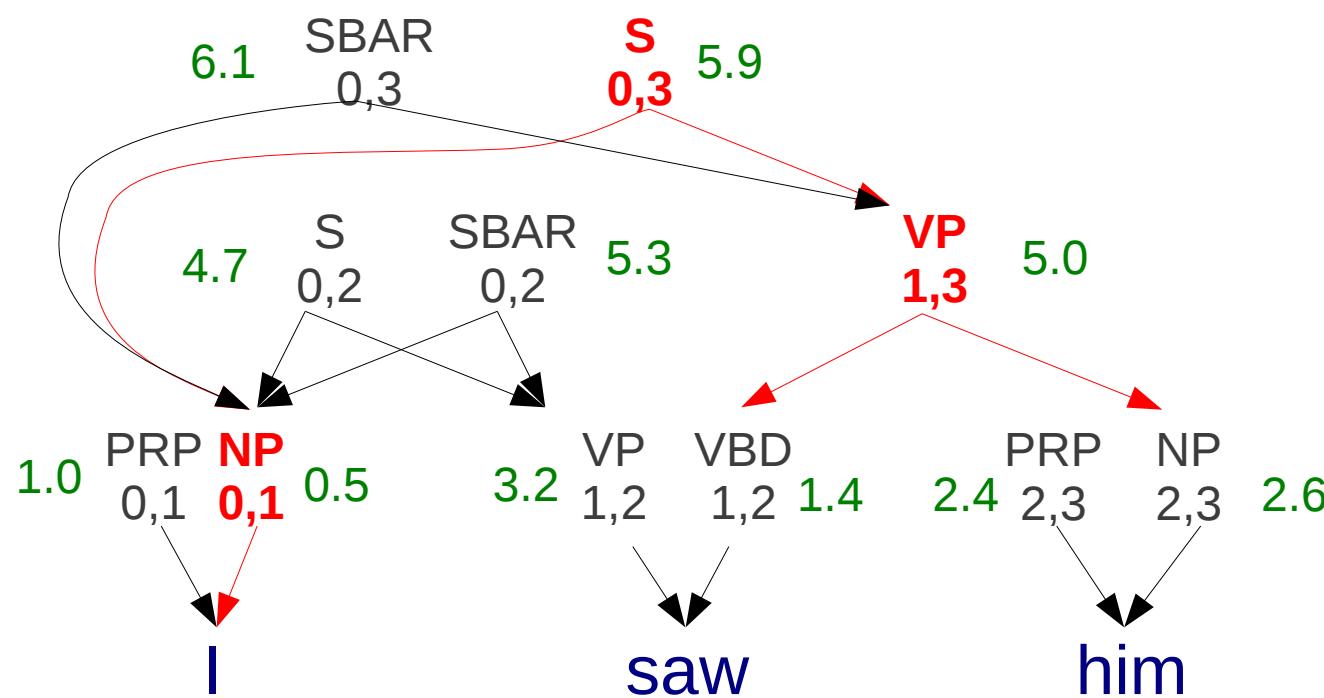
# CKY Algorithm

- Expand the left child, right child recursively until we have our tree



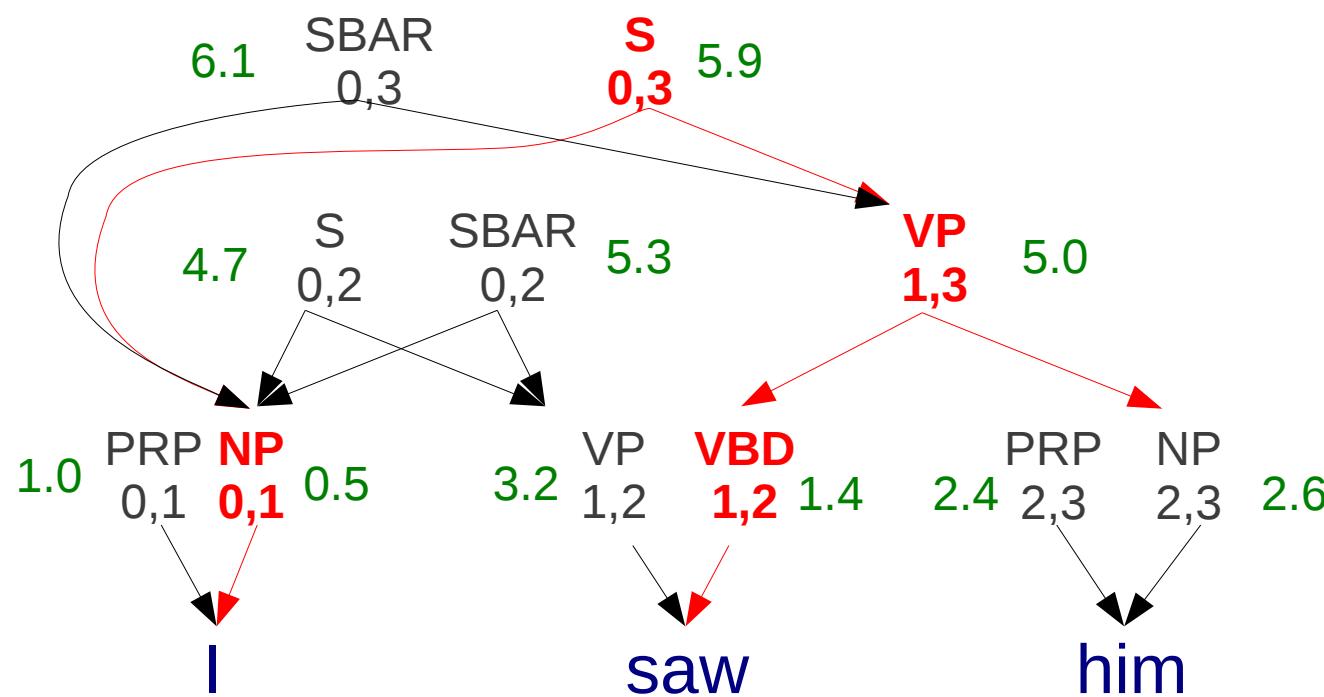
# CKY Algorithm

- Expand the left child, right child recursively until we have our tree



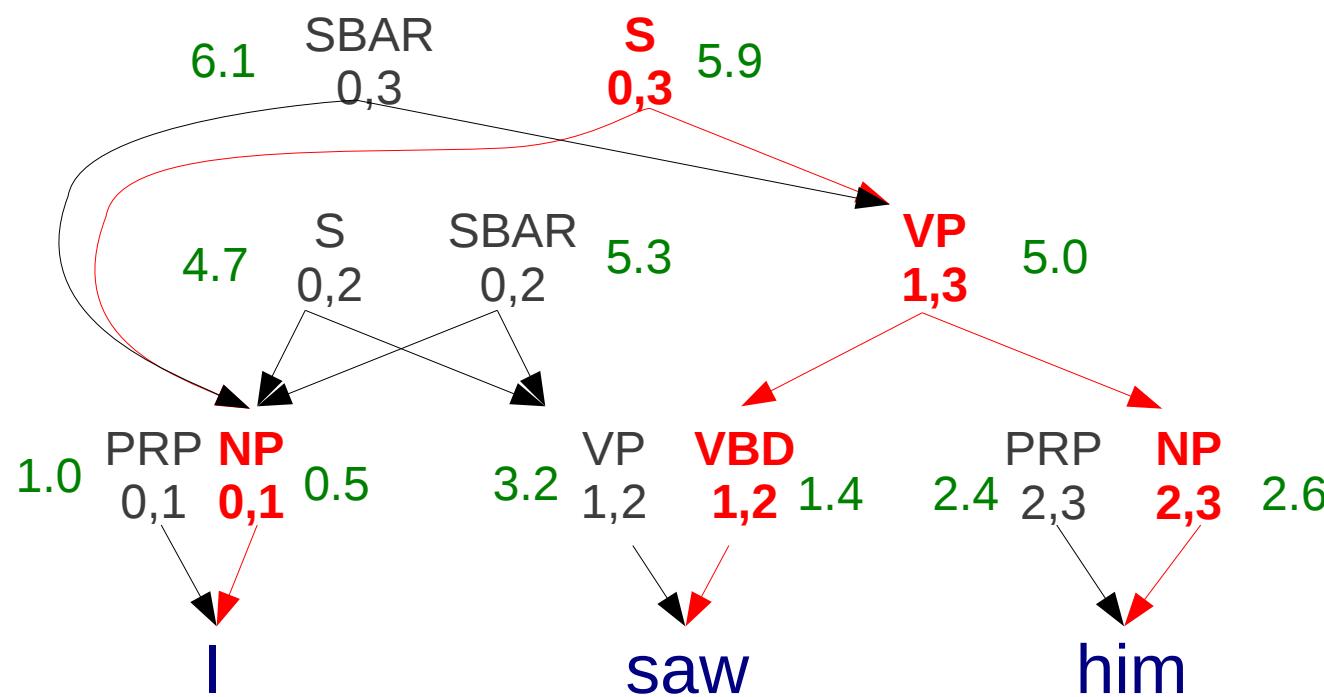
# CKY Algorithm

- Expand the left child, right child recursively until we have our tree



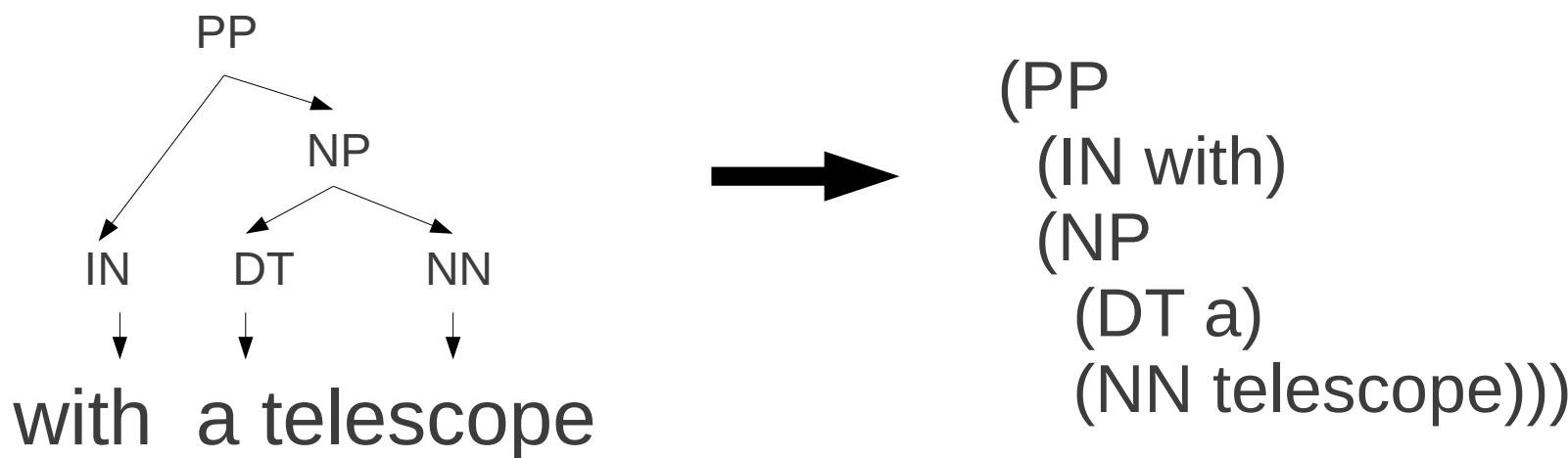
# CKY Algorithm

- Expand the left child, right child recursively until we have our tree



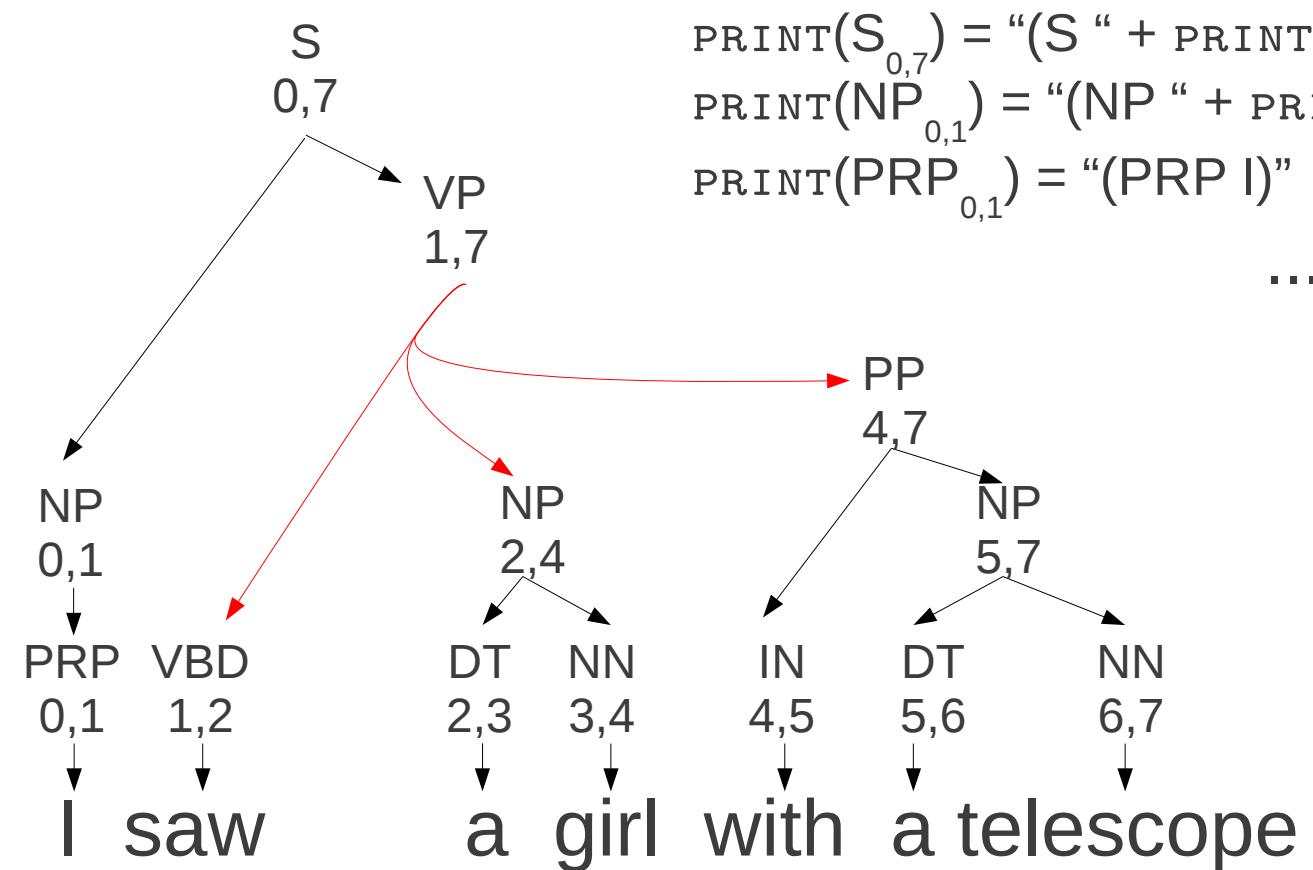
# Printing Parse Trees

- Standard text format for parse tree: “Penn Treebank”



# Printing Parse Trees

- Hypergraphs printed recursively, starting at top:



$\text{PRINT}(S_{0,7}) = "(S " + \text{PRINT}(NP_{0,1}) + " " + \text{print}(VP_{1,7}) + ")"$   
 $\text{PRINT}(NP_{0,1}) = "(NP " + \text{PRINT}(PRP_{0,1}) + ")"$   
 $\text{PRINT}(PRP_{0,1}) = "(PRP I)"$

...

# Pseudo-Code

# CKY Pseudo-Code: Read Grammar

```
# Read a grammar in format "lhs \t rhs \t prob \n"
make list nonterm # Make list of (lhs, rhs1, rhs2, prob)
make map preterm # Make a map preterm[rhs] = [ (lhs, prob) ...]
for rule in grammar_file
    split rule into lhs, rhs, prob (with "\t") # Rule P(lhs → rhs)=prob
    split rhs into rhs_symbols (with " ")
    if length(rhs) == 1: # If this is a pre-terminal
        add (lhs, log(prob)) to preterm[rhs]
    else: # Otherwise, it is a non-terminal
        add (lhs, rhs[0], rhs[1], log(prob)) to nonterm
```

# CKY Pseudo-Code: Add Pre-Terminals

```
split /line into words
make map best_score # index: symi,j value = best log prob
make map best_edge # index: symi,j value = (lsymi,k, rsymk,j)
# Add the pre-terminal sym
for i in 0 .. length(words)-1:
    for lhs, log_prob in preterm where P(lhs → words[i]) > 0:
        best_score[lhsi,i+1] = [log_prob]
```

# CKY Pseudo-Code: Combine Non-Terminals

```
for j in 2 .. length(words): # j is right side of the span
    for i in j-2 .. 0:          # i is left side (Note: Reverse order!)
        for k in i+1 .. j-1:    # k is beginning of the second child
            # Try every grammar rule log(P(sym → lsym rsym)) = logprob
            for sym, lsym, rsym, logprob in nonterm:
                # Both children must have a probability
                if best_score[lsymi,k] > -∞ and best_score[rsymk,j] > -∞:
                    # Find the log probability for this node/edge
                    my_lp = best_score[lsymi,k] + best_score[rsymk,j] + logprob
                    # If this is the best edge, update
                    if my_lp > best_score[symi,j]:
                        best_score[symi,j] = my_lp
                        best_edge[symi,j] = (lsymi,k, rsymk,j)
```

# CKY Pseudo-Code: Print Tree

```
PRINT( $S_{0,\text{length(words)}}$ ) # Print the “S” that spans all words
```

```
subroutine PRINT(symi,j):  
    if symi,j exists in best_edge: # for non-terminals  
        return “(+sym+“ “  
            + PRINT(best_edge[0]) + “ ” +  
            + PRINT(best_edge[1]) + “)”  
else: # for terminals  
    return “(+sym+“ ”+words[i]+“)”
```

# Exercise

# Exercise

- Write cky.py
- Test the program
  - Input: test/08-input.txt
  - Grammar: test/08-grammar.txt
  - Answer: test/08-output.txt
- Run the program on actual data:
  - data/wiki-en-test.grammar, data/wiki-en-short.tok
- Visualize the trees
  - script/print-trees.py < wiki-en-test.trees
  - (Requires NLTK: <http://nltk.org/>)
- Challenge: think of a way to handle unknown words

# Thank You!